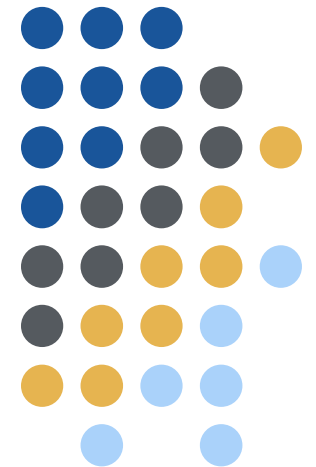


Design-Oriented Characterization of Uncertainty in Computed Axial Capacities of Deep Foundation Members

STGEC | Tue. Oct. 18, 2022 | 1130 AM - 12 PM

Michael Davidson, PhD, PE
Bridge Software Institute
University of Florida





Outline

- Introduction
- Characterization of spatial variability
- Illustration case
- Summary



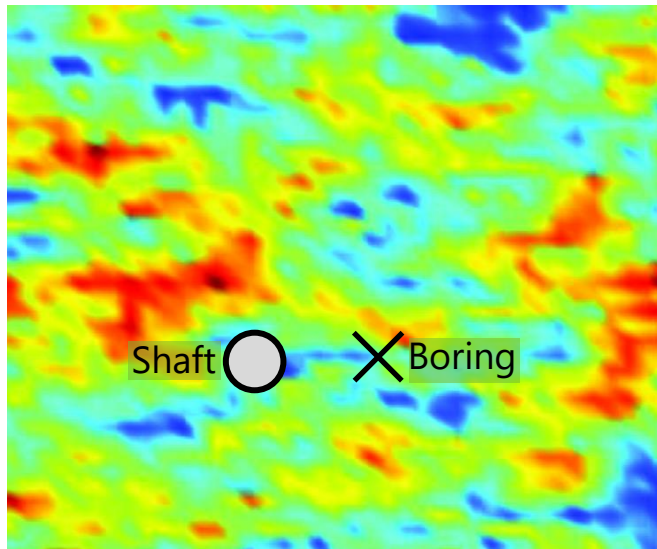
Outline

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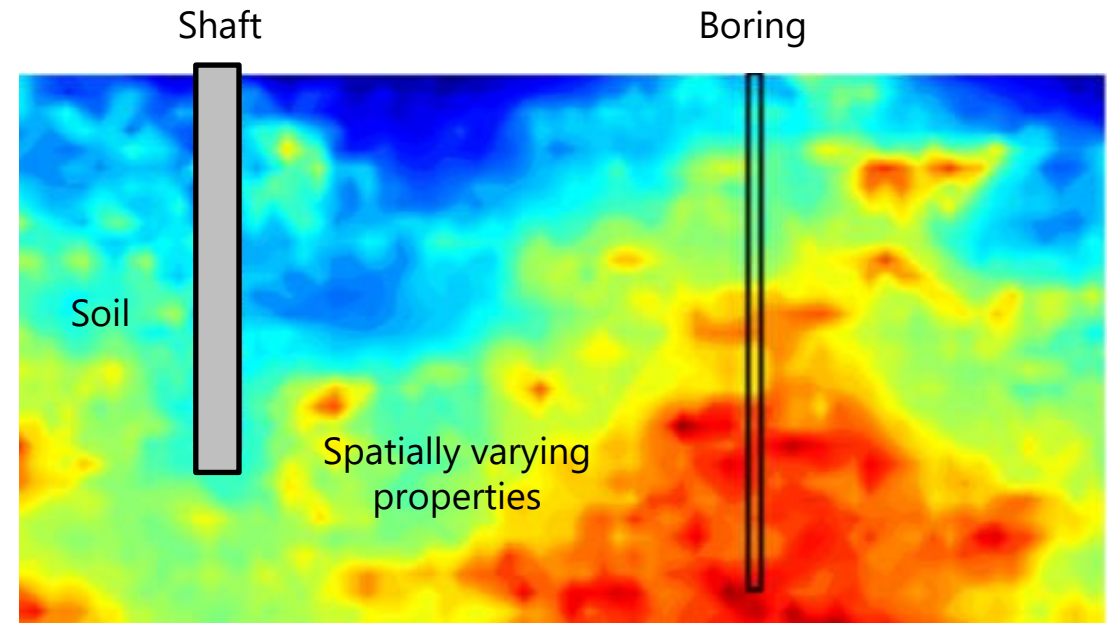


Introduction

- Spatial variability
 - Horizontal
 - Vertical



Plan view, illustrative
(contour image from Zhu and Zang 2013)

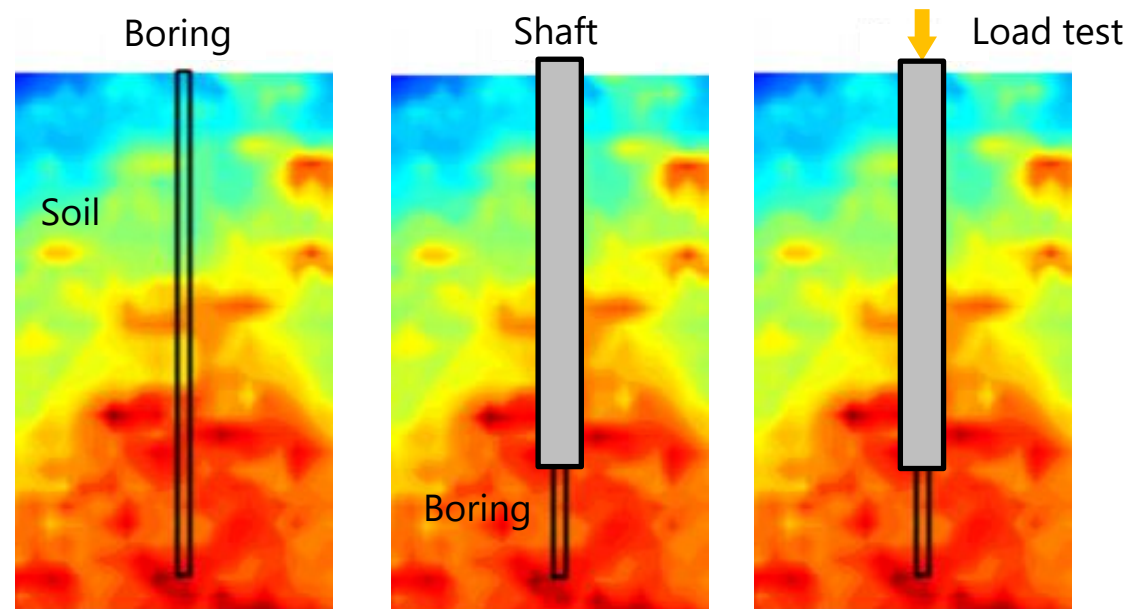


Elevation view, illustrative
(contour image from McVay et al. 2012)



Introduction

- Method error
 - Due to underlying assumptions in empirical methods
 - Correlation of measurement to unit resistance

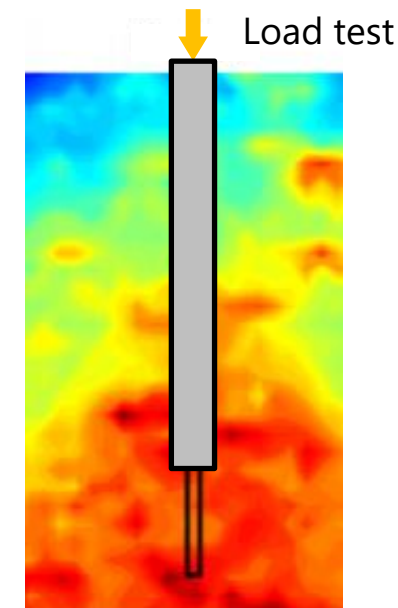
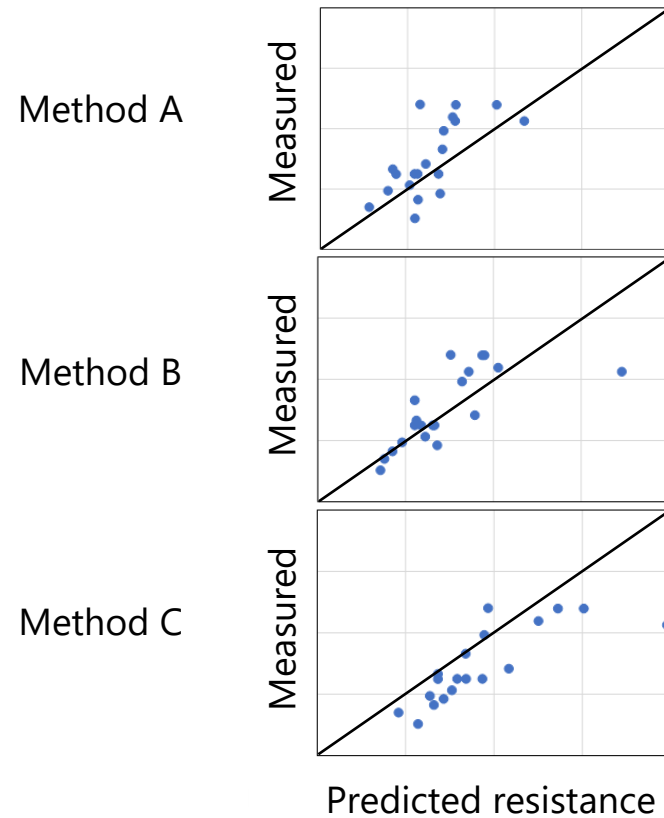


Example: boring in footprint of shaft

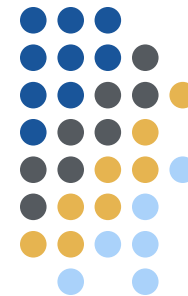


Introduction

- Method error
 - Increases uncertainty in computed capacities

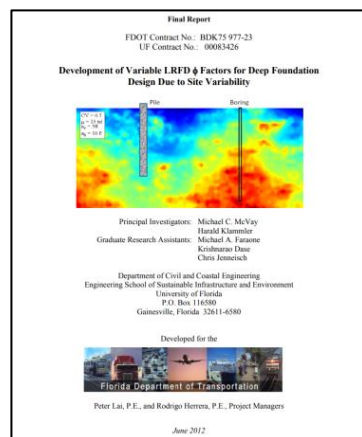


Example: boring in footprint of shaft

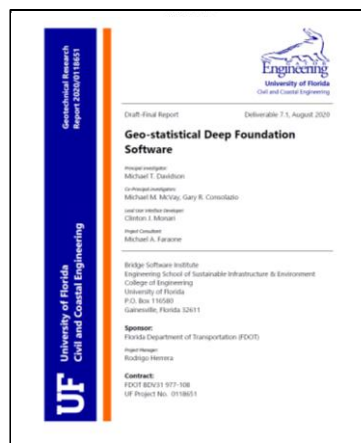


Previous research efforts

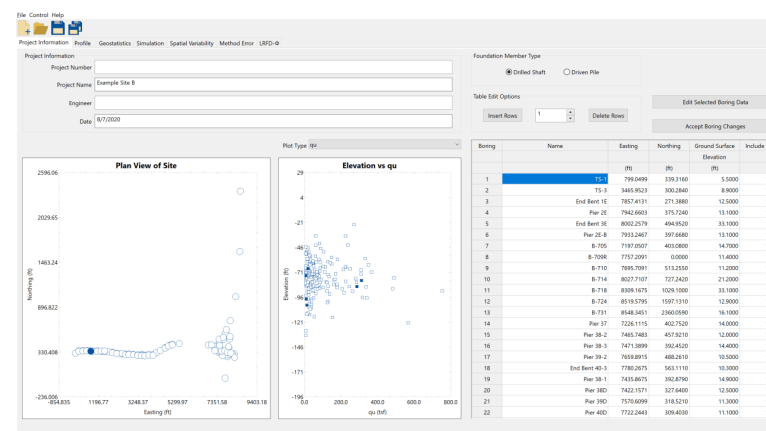
- FDOT BDK 977-23, BDV31 977-108, BDV31 977-143
 - Formulated geostatistical methodologies
 - Compiled method error data
 - Developed prototype and design tools



FDOT BDK75 977-23 final report



FDOT BDV31 977-108 final report



GeoStat design tool





Motivation

- How do variability and uncertainty affect design?



Motivation

- How do variability and uncertainty affect design?
 - Example: resistance factors

$$\phi = \frac{\lambda_R \left(\gamma_D \cdot \frac{Q_D}{Q_L} + \gamma_L \right) \cdot \sqrt{\frac{1 + COV_{QD}^2 + COV_{QL}^2}{1 + COV_R^2}}}{\left(\lambda_{QD} \cdot \frac{Q_D}{Q_L} + \lambda_{QL} \right) \cdot \exp \left(\beta \cdot \sqrt{\ln \left((1 + COV_R^2) \cdot (1 + COV_{QD}^2 + COV_{QL}^2) \right)} \right)}$$

Resistance factor, ϕ , NCHRP 507

Term description	Symbol	Value
Dead load factor	γ_D	1.25
Live load factor	γ_L	1.75
Dead to live load ratio	Q_D/Q_L	2.00
Dead load bias factor	λ_{QD}	1.08
Live load bias factor	λ_{QL}	1.15
Mean resistance bias factor	λ_R	1.0
Dead load coefficient of variation	COV_{QD}	0.128
Live load coefficient of variation	COV_{QL}	0.18
Target reliability index	β	3.0

Illustrative values of component terms for evaluation of LRFD resistance factors, ϕ



Motivation

- How do variability and uncertainty affect design?
 - Example: resistance factors

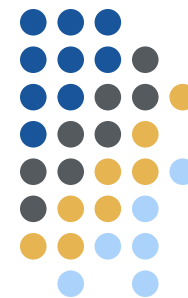
$$\phi = \frac{\lambda_R \left(\gamma_D \cdot \frac{Q_D}{Q_L} + \gamma_L \right) \cdot \sqrt{\frac{1 + COV_{QD}^2 + COV_{QL}^2}{1 + COV_R^2}}}{\left(\lambda_{QD} \cdot \frac{Q_D}{Q_L} + \lambda_{QL} \right) \cdot \exp \left(\beta \cdot \sqrt{\ln \left((1 + COV_R^2) \cdot (1 + COV_{QD}^2 + COV_{QL}^2) \right)} \right)}$$

Resistance factor, ϕ , NCHRP 507

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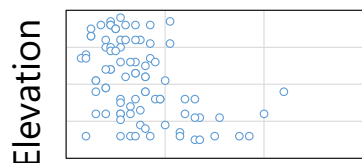
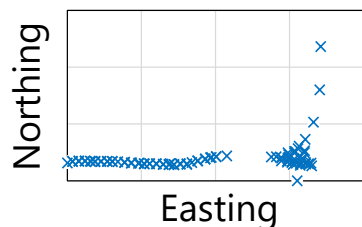
Illustrative values of component terms for evaluation of LRFD resistance factors, ϕ

COV_R : Coefficient of variation in resistance

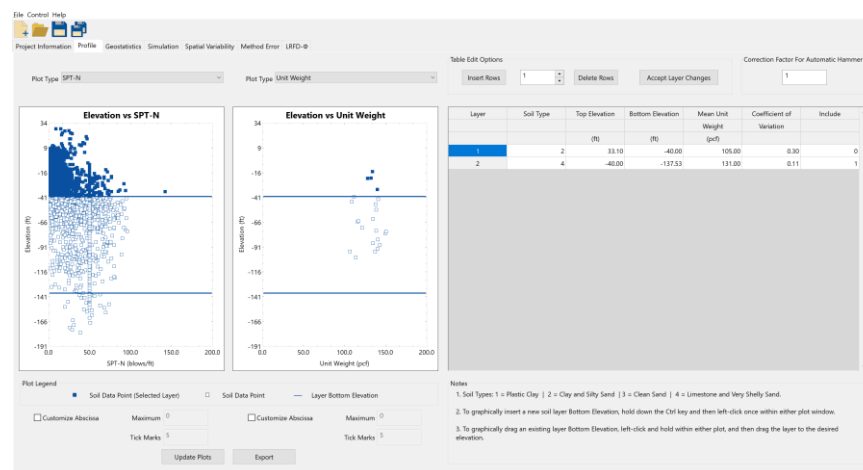


Motivation

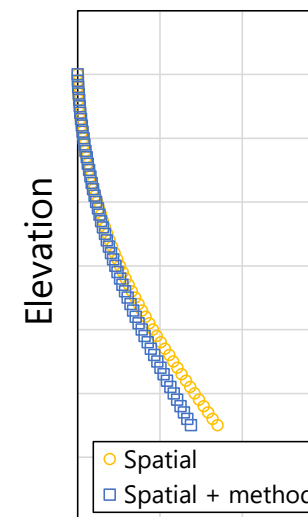
- Direct incorporation of variability and uncertainty can benefit foundation design
 - Assess sufficiency of available site data
 - More uniform levels of conservatism
 - Site-specific reflection of variability



Site measurements



Illustrative layer definitions in GeoStat



Computed resistance

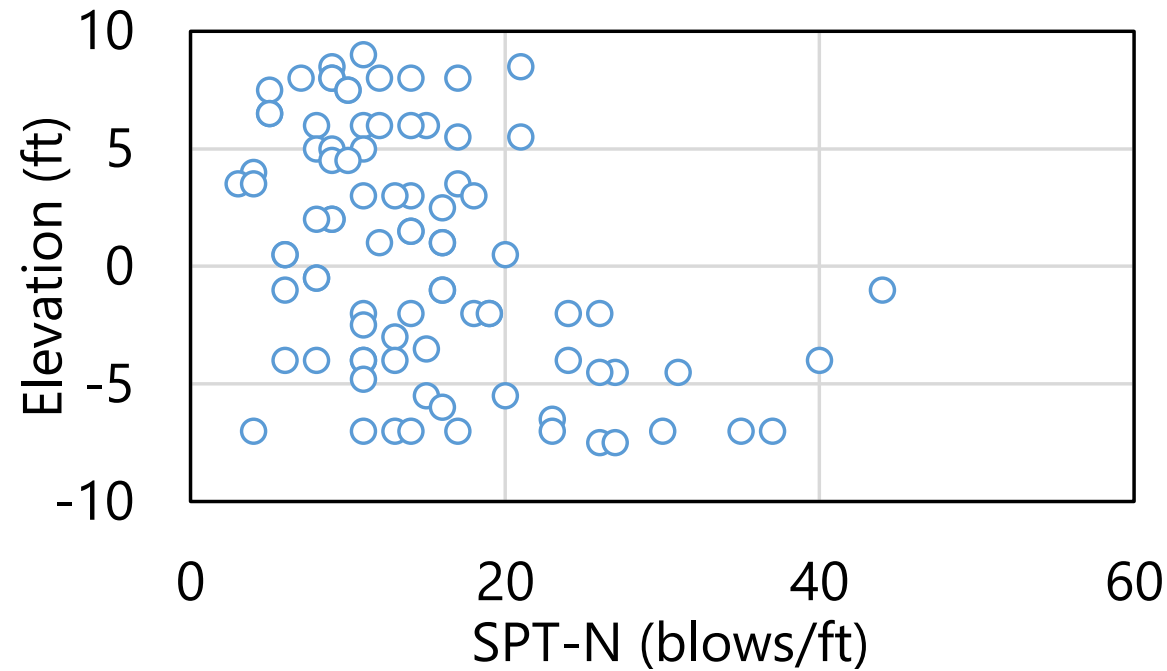


Outline

- Introduction
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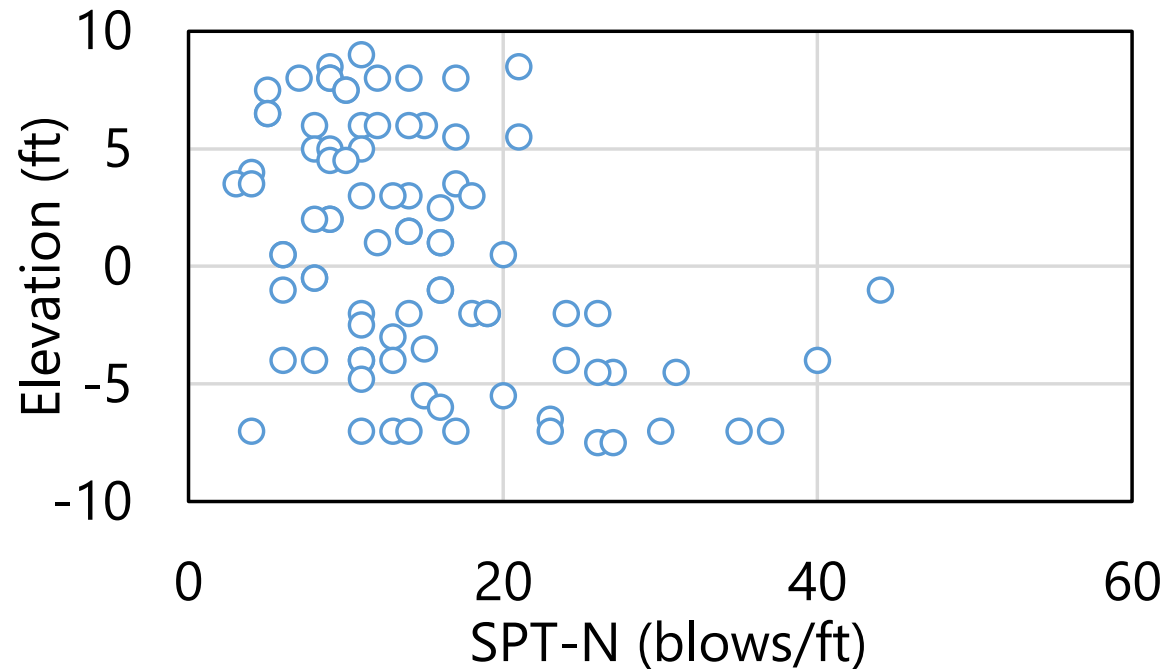
Consider a set of 88 SPT-N values



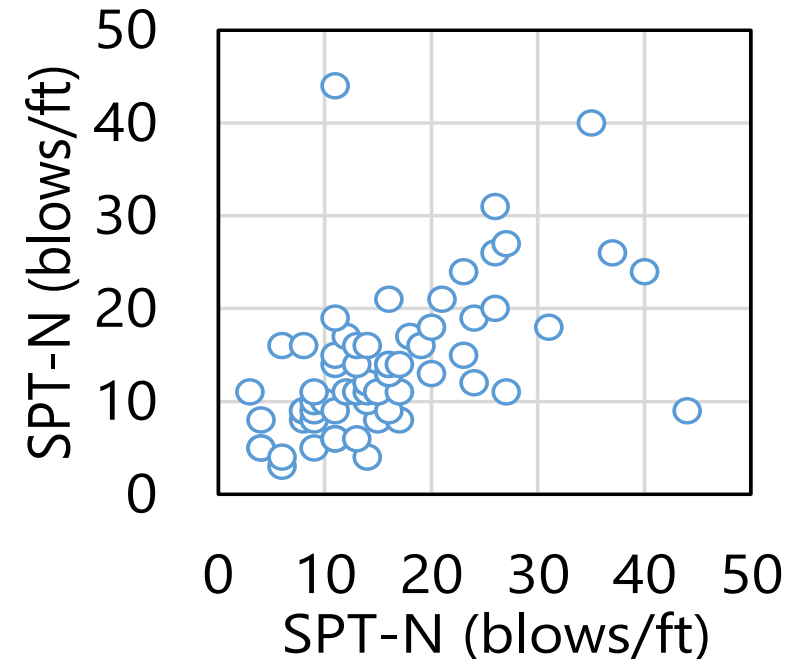
Illustrative collection of 88 SPT-N values



Examine pairs of values 2.5 ft apart



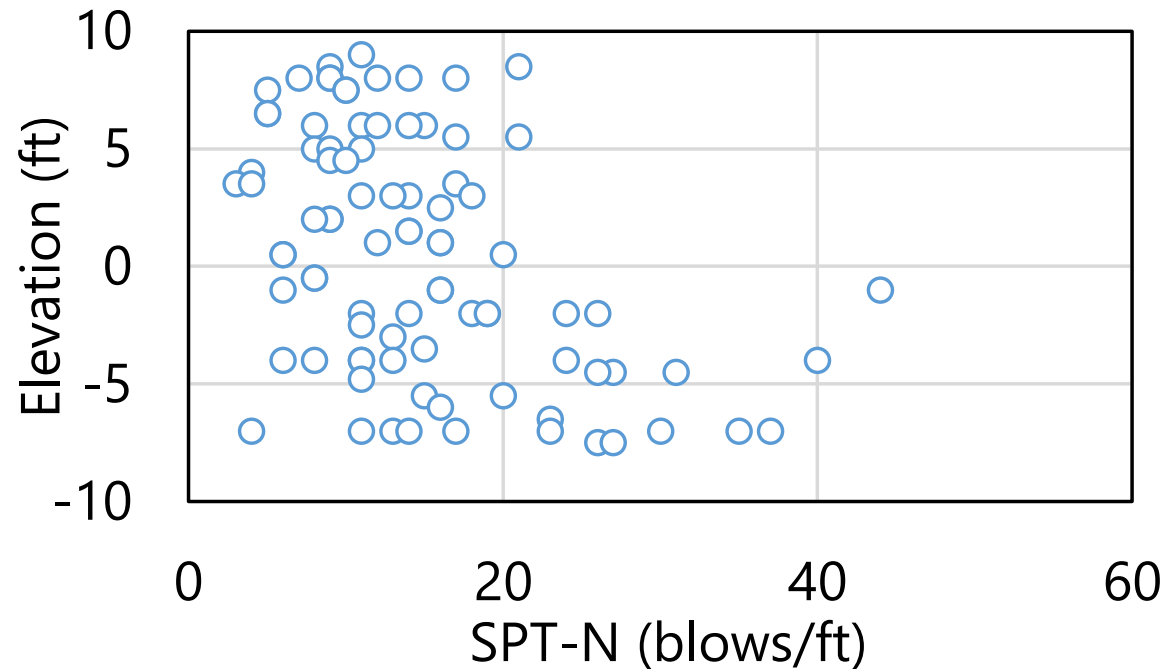
Illustrative collection of 88 SPT-N values



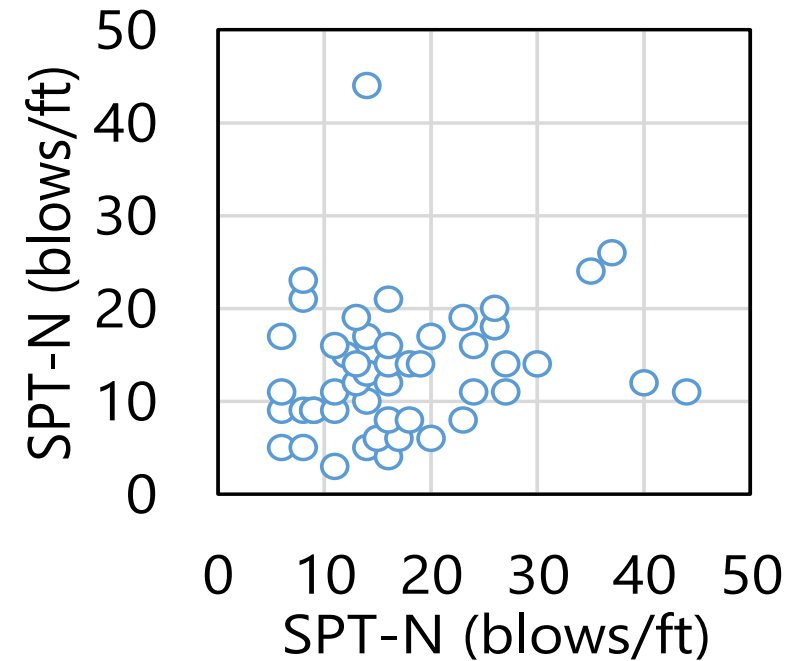
Pairs that lie 2.5 ft apart



Examine pairs of values 5.0 ft apart



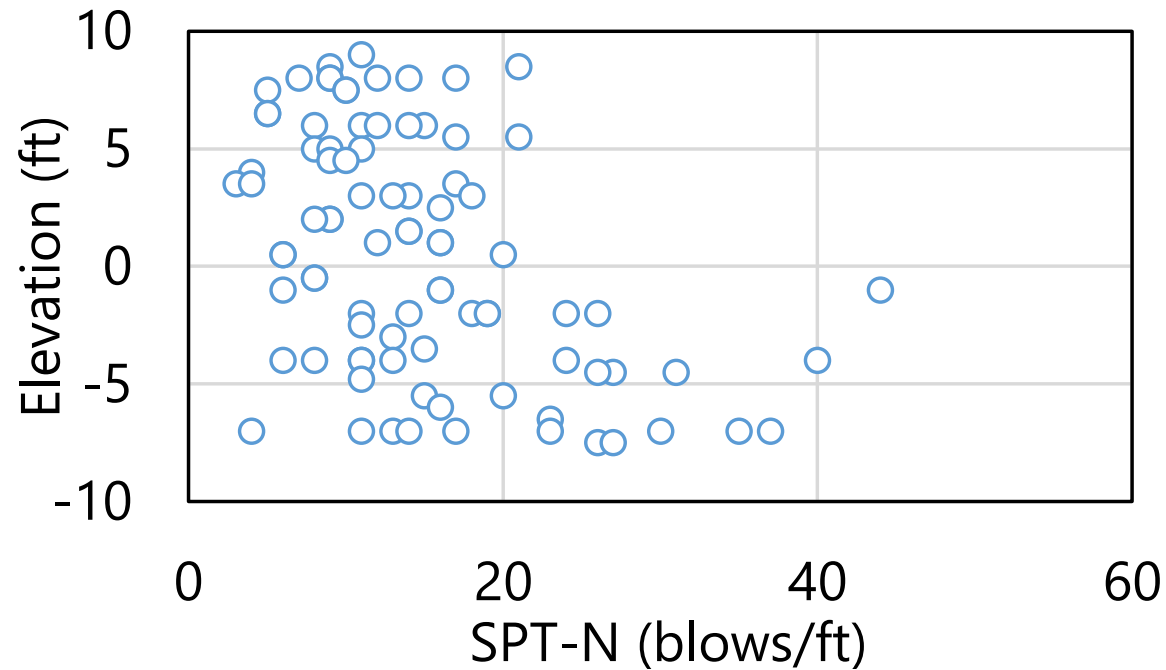
Illustrative collection of 88 SPT-N values



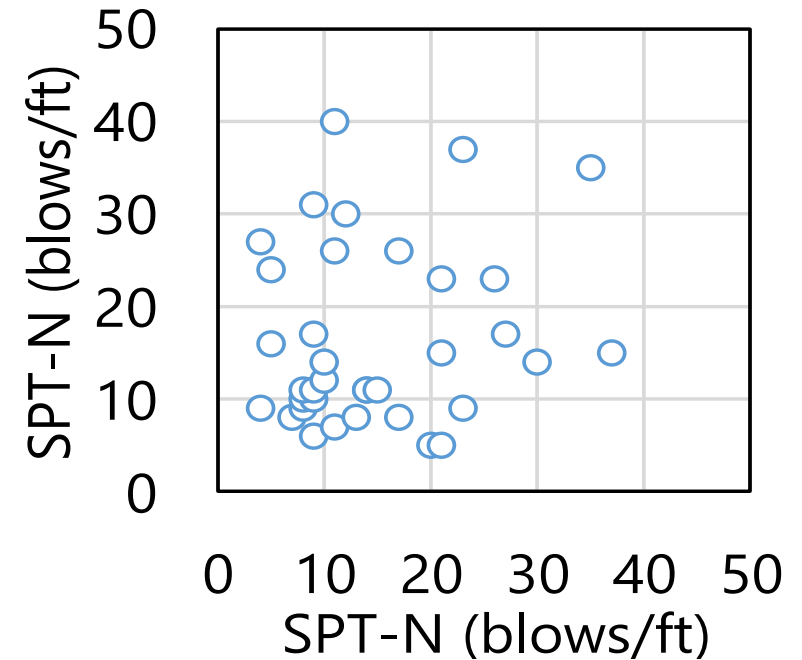
Pairs that lie 5.0 ft apart



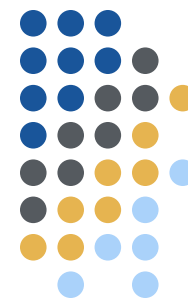
Examine pairs of values 12.5 ft apart



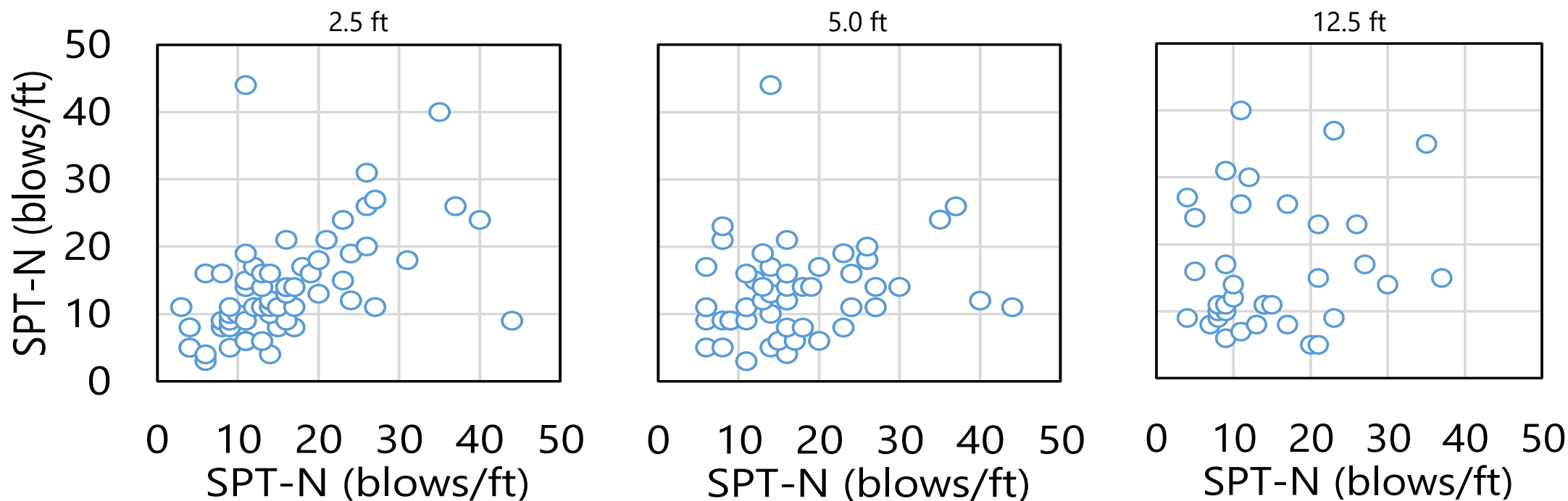
Illustrative collection of 88 SPT-N values



Pairs that lie 12.5 ft apart



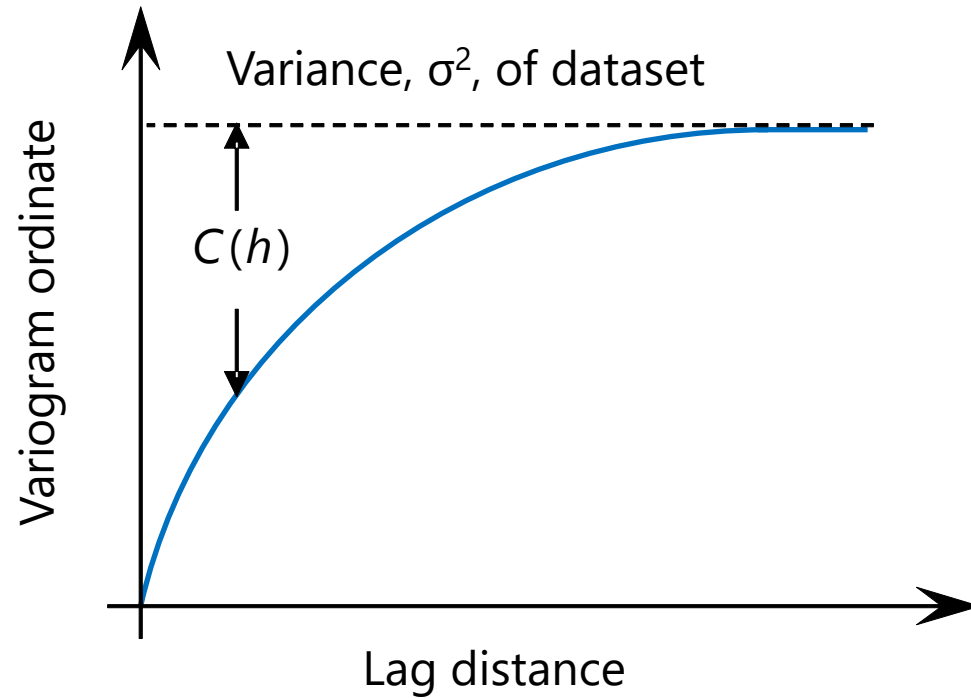
Strength of correlation and covariance vary with respect to distance (h)



Covariance:
$$C(h) = \frac{1}{n_{pairs}} \sum_{i,j=1}^{n_{pairs}} (SPT_i - Mean)^2 \cdot (SPT_j - Mean)^2$$



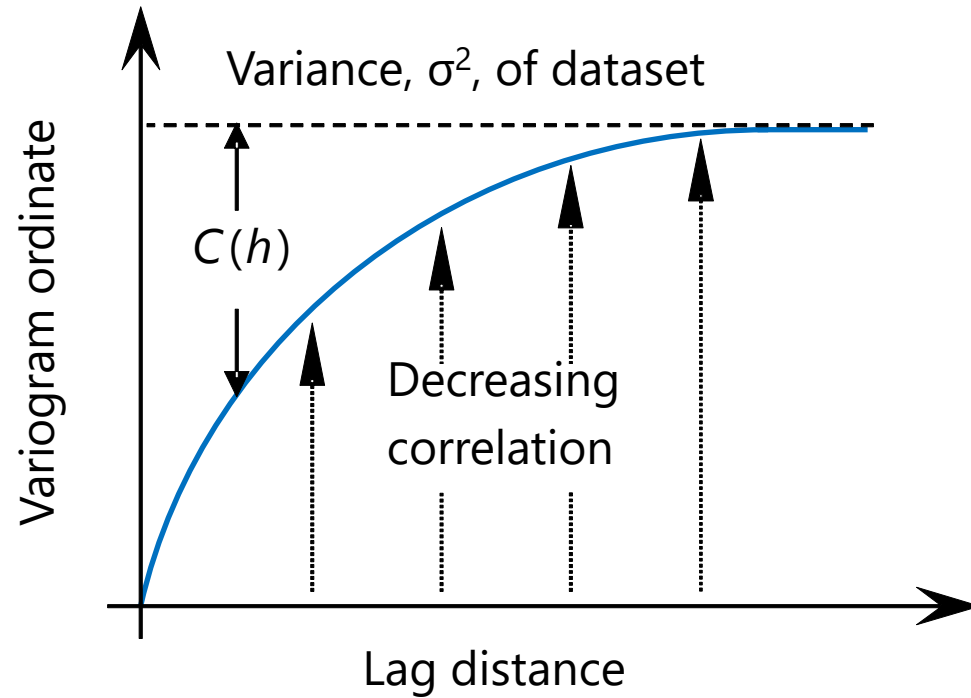
Variograms compactly express spatial variability phenomena



Variogram: $v(h) = \sigma^2 - C(h)$



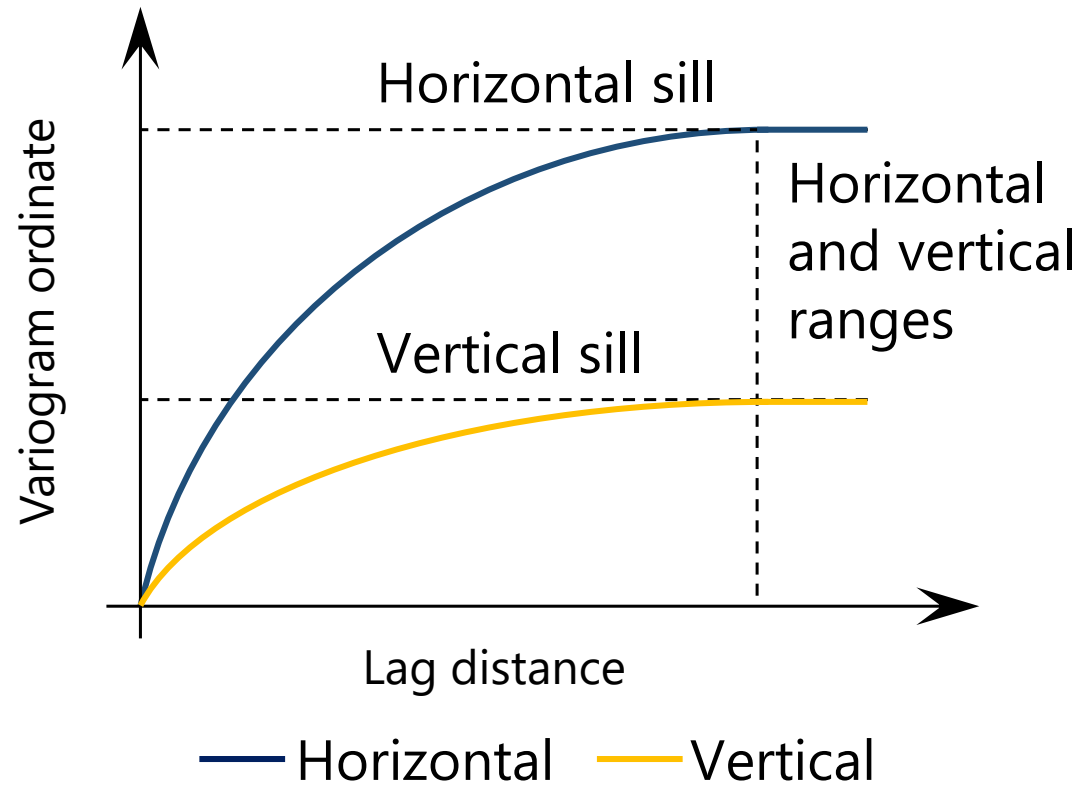
Variograms compactly express spatial variability phenomena

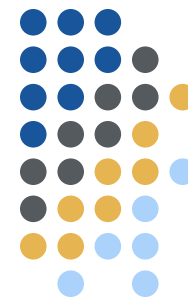


Distance between any two measurements (h)

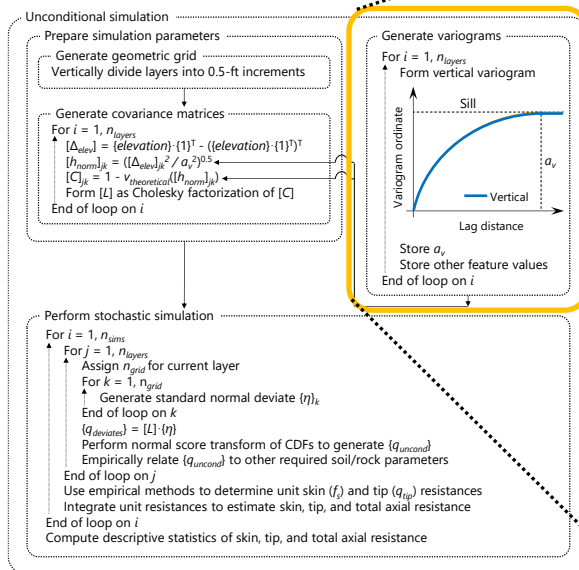


Variograms can reveal geological zones





Variograms are necessary for geostatistical simulation



Geostatistical simulation algorithm

Prepare simulation parameters

Generate geometric grid
Vertically divide layers into 0.5-ft increments

Generate covariance matrices

For $i = 1, n_{layers}$

$$[\Delta_{elev}] = \{elevation\} \cdot \{1\}^T - (\{elevation\} \cdot \{1\}^T)^T$$

$$[h_{norm}]_{jk} = ([\Delta_{elev}]_{jk}^2 / a_v^2)^{0.5}$$

$$[C]_{jk} = 1 - v_{theoretical}([h_{norm}]_{jk})$$

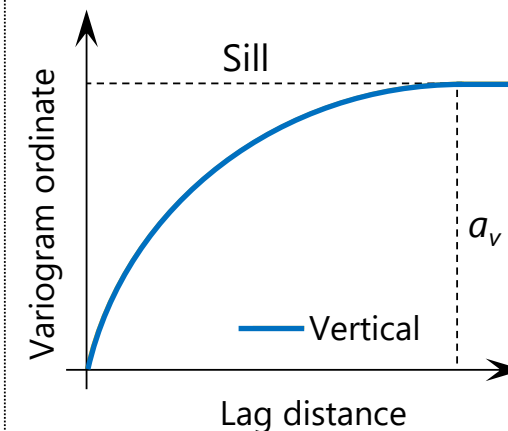
Form $[L]$ as Cholesky factorization of $[C]$

End of loop on i

Generate variograms

For $i = 1, n_{layers}$

Form vertical variogram



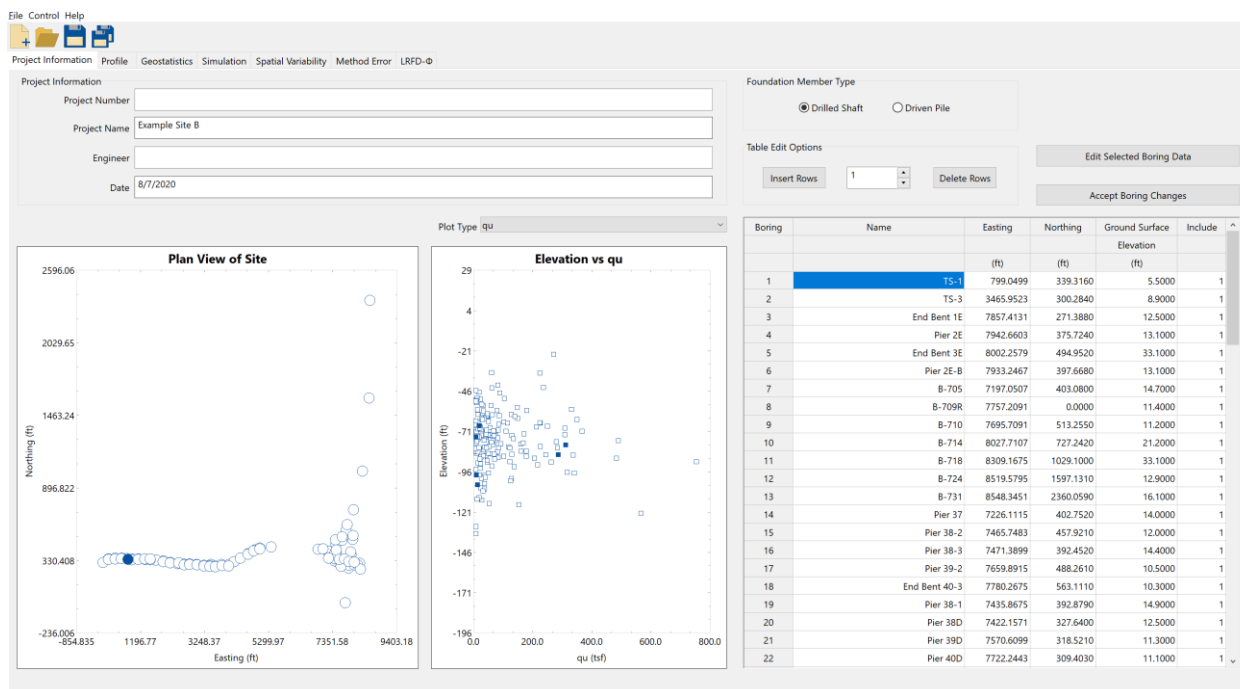
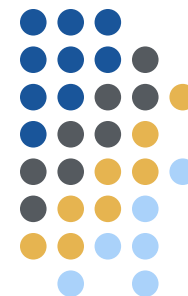
Store a_v
Store other feature values
End of loop on i



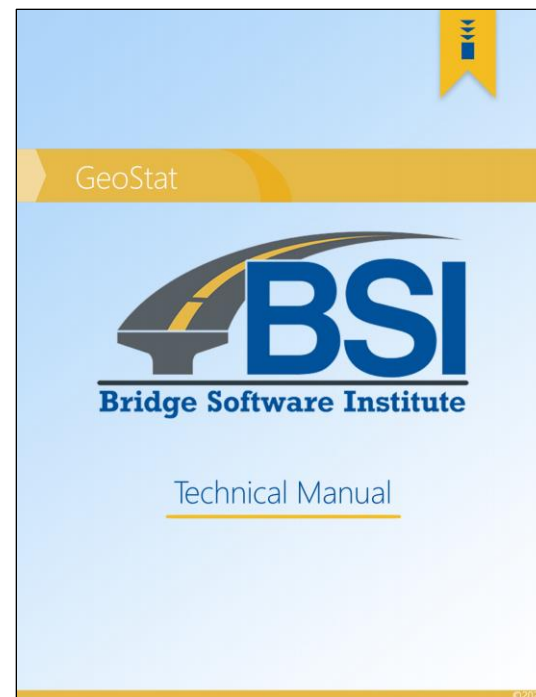
Outline

- Introduction
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Use geostatistical tool to assess shaft axial capacities within an example site



GeoStat software



GeoStat technical manual (Ch. 5)

CHAPTER 5 MODELING OF EXAMPLE SITE B

5.1 Overview

Presented in Ch. 5 is a second, detailed walkthrough of geotechnical site modeling and axial resistance simulation for an example bridge site. The data sets discussed in Ch. 5 represent one instance of the ranges and types of geotechnical site data that may be collected when investigating the foundations of a bridge site possessing medium variability. An example site exhibiting high variability is discussed in Ch. 4. In addition, the extent or size of the site of interest in Ch. 5 is large relative to that discussed in Ch. 4. Within the context of modeling and simulation in GeoStat, use of the associated (medium variability, large extent) site data is divided into several steps. Such division reflects the left-to-right progression across the seven tabs of the GeoStat user interface (UI), where the layout of the GeoStat UI is detailed in the program Help Manual.

The site of interest in Ch. 5 is referred to as Example Site B, or, Site B. Cataloging of the available Site B data for modeling within GeoStat is discussed in Sec. 5.2. Initial selection of boundary soil and rock (limestone) layer elevations is discussed in Sec. 5.3. Also documented in Sec. 5.3 are layer-related considerations specific to the type of foundation member being considered (pile, shaft).

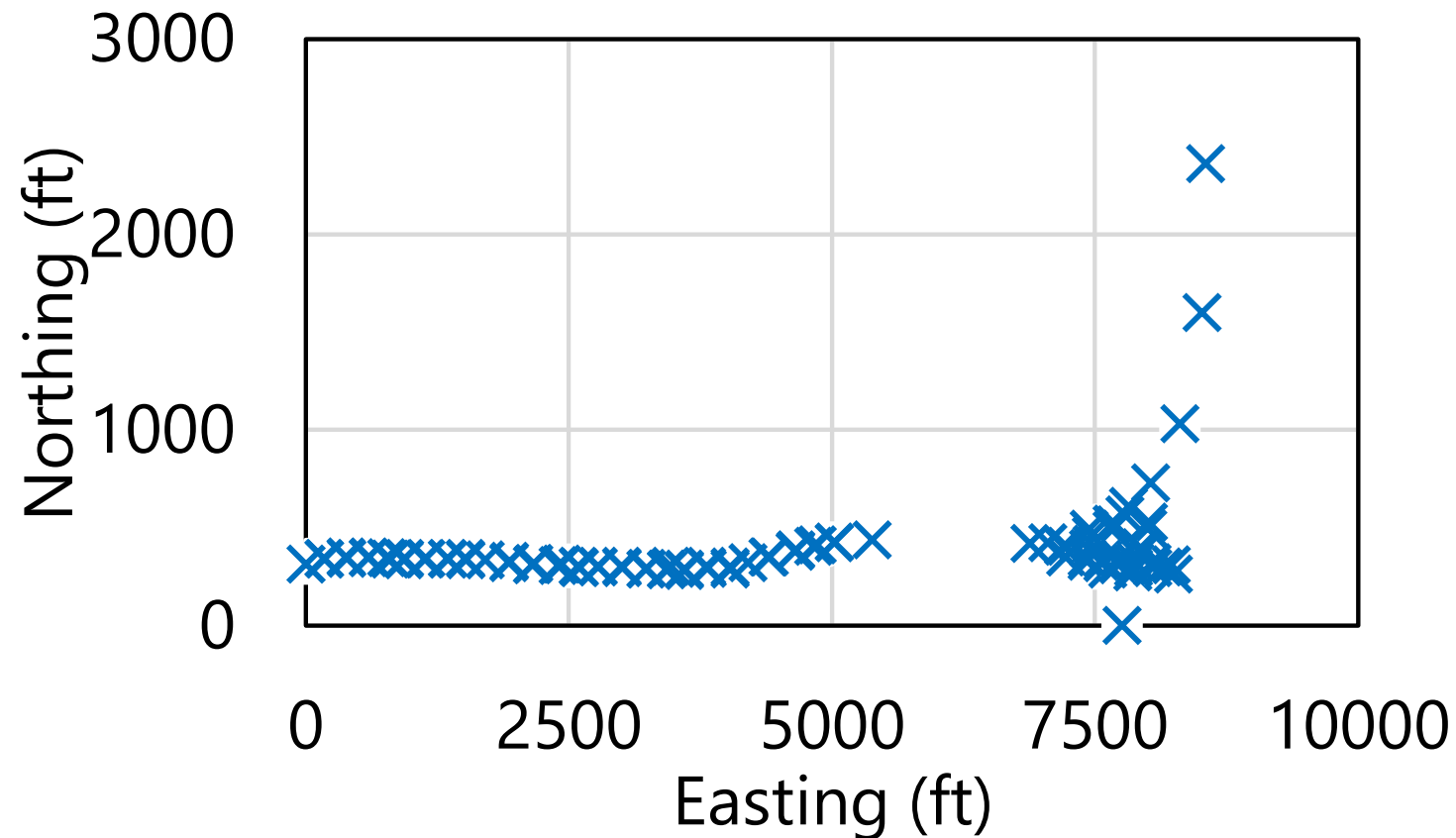
Initial formation of spatial correlation structures (i.e., variograms) for each defined layer, and solely for the purpose of identifying geological zones, is then discussed in Sec. 5.4. Observations and considerations related to the identification of geological zones within Site B are discussed in Sec. 5.5. These considerations include assessment of zonal anisotropy and illustration of how zones are defined (modeled) within GeoStat. Two zones are identified among the Site B data set, where detailed walkthroughs of characterizing zone-specific layer definitions and variograms are illustrated in Sec. 5.6 (for zone 1) and Sec. 5.7 (for zone 2). For each of the two illustrations, comparisons are made to respective quantities obtained from the site-wide data set to demonstrate the importance of accounting for geological zones. Summary observations regarding the site-wide, zone 1, and zone 2 data sets (with respect to variograms) are provided in Sec. 5.8.

The focus of the walkthrough for Site B then shifts to stochastic simulation of axial resistance in Sec. 5.9, where one set of simulations is conducted for each of zone 1 and zone 2. Interpretation of simulated profiles of axial resistance, which reflect spatial variability phenomena of the zone-specific data, is provided in Sec. 5.10.

Comparisons are subsequently made between zone-specific simulation results to further emphasize the importance of accounting for distinct geological zones. Considerations for incorporating method error phenomena into the simulated, zone-specific results are detailed

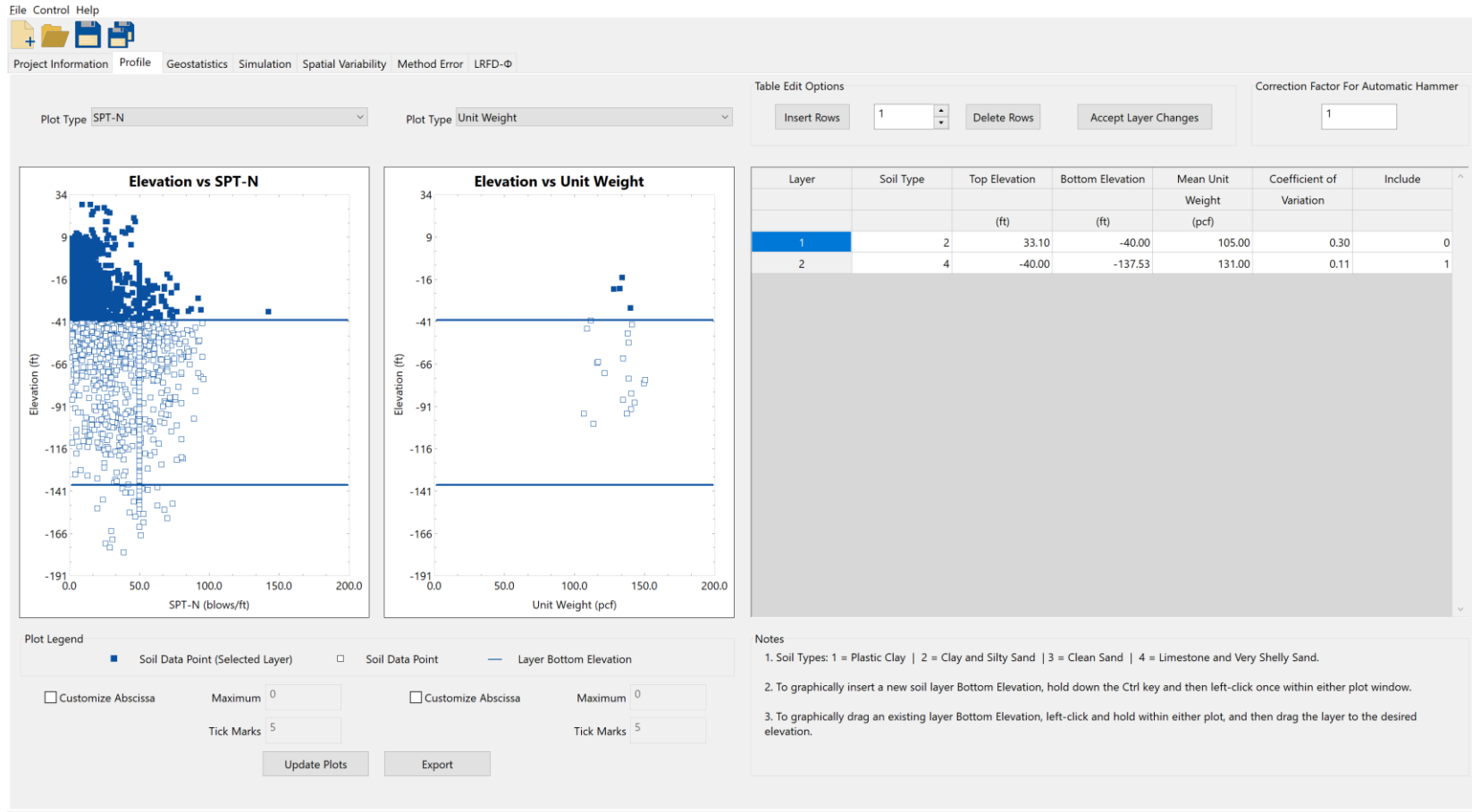


Consider a site with 90 boring locations





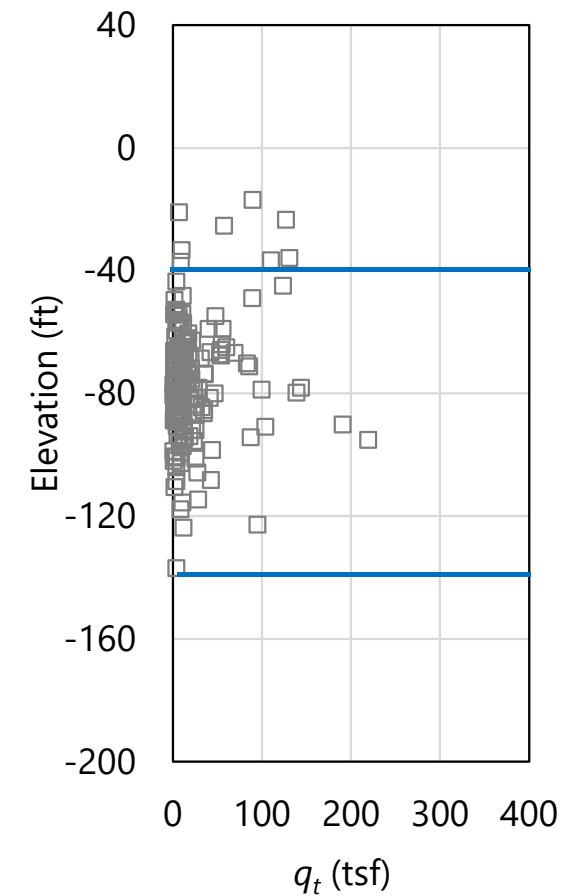
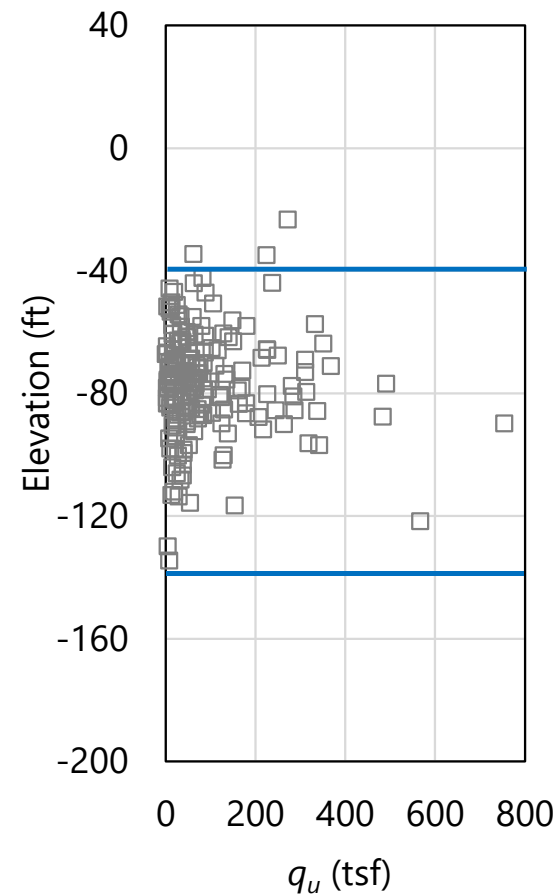
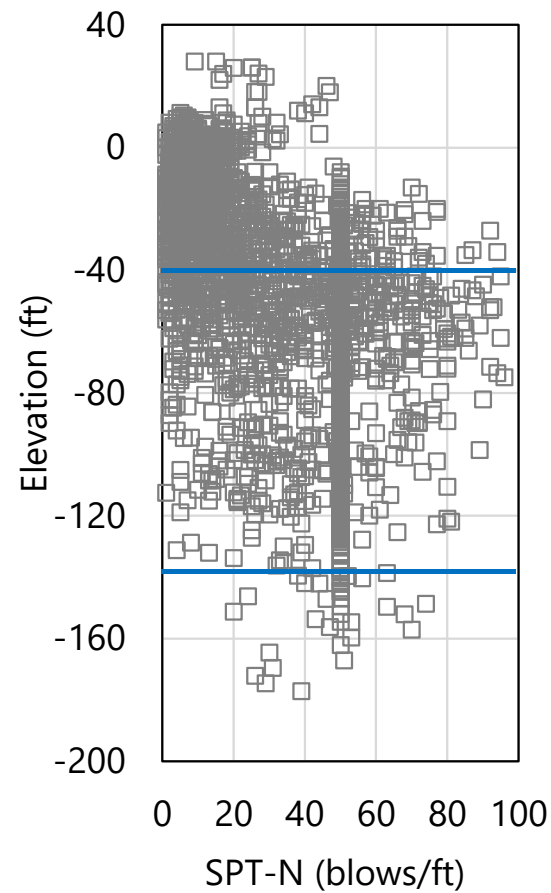
Determine layering



GeoStat – Profile tab

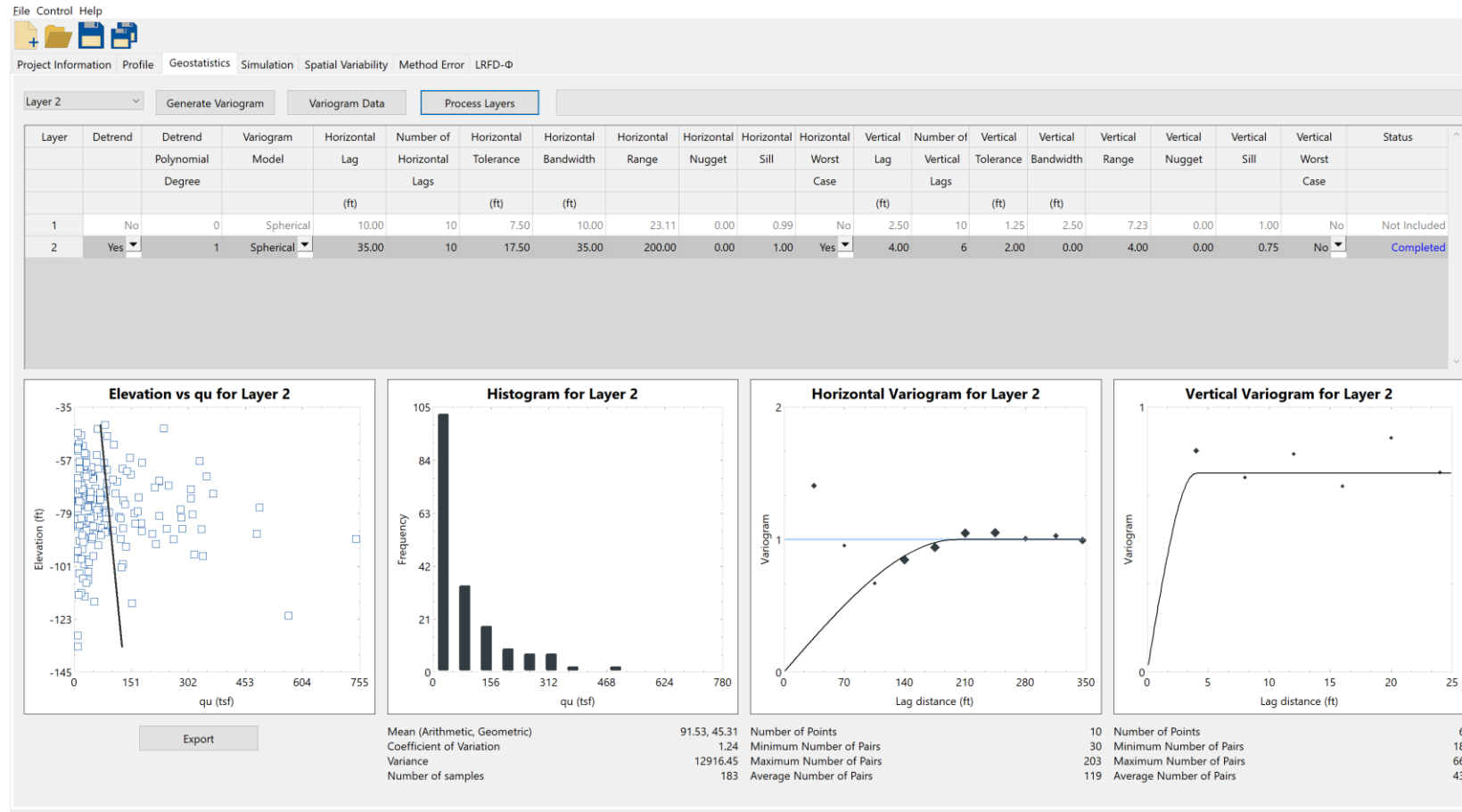


Determine layering





Form horizontal and vertical variograms for each layer



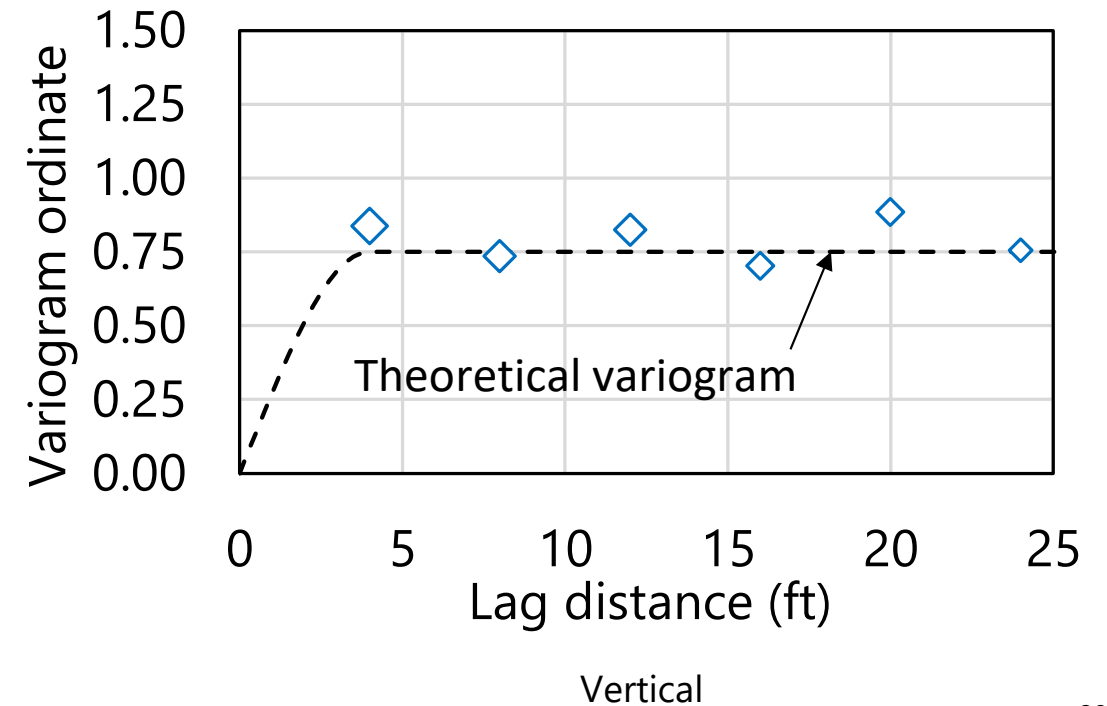
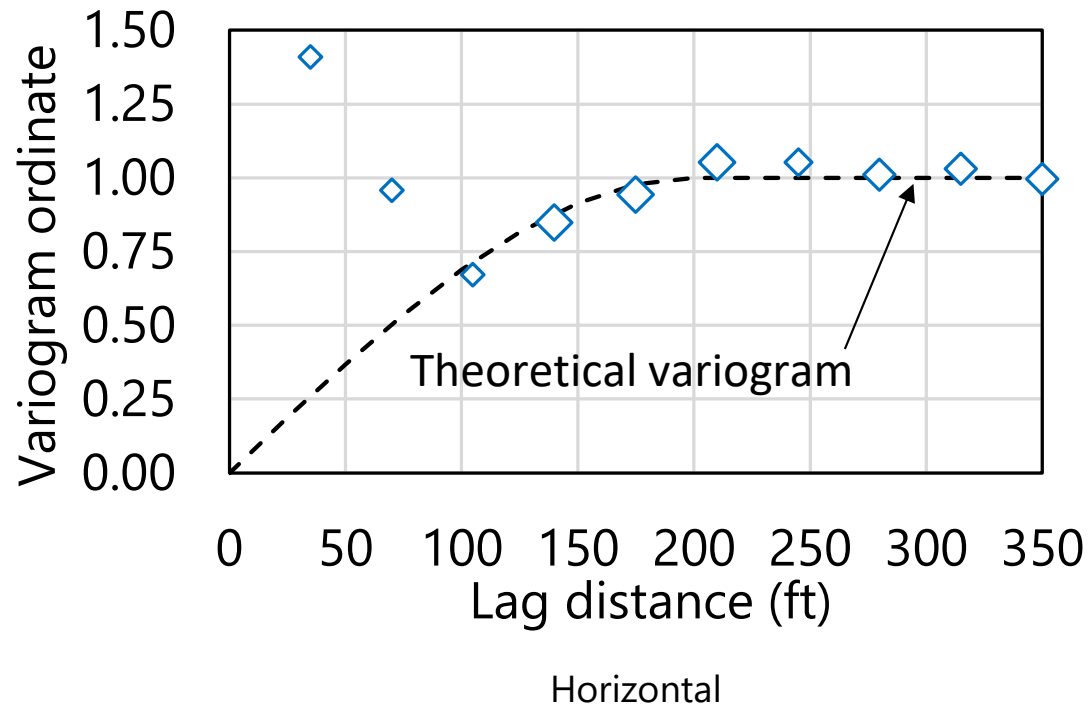
Technical Manual - Chs. 2, 5

GeoStat – Geostatistics tab



Inspect variograms

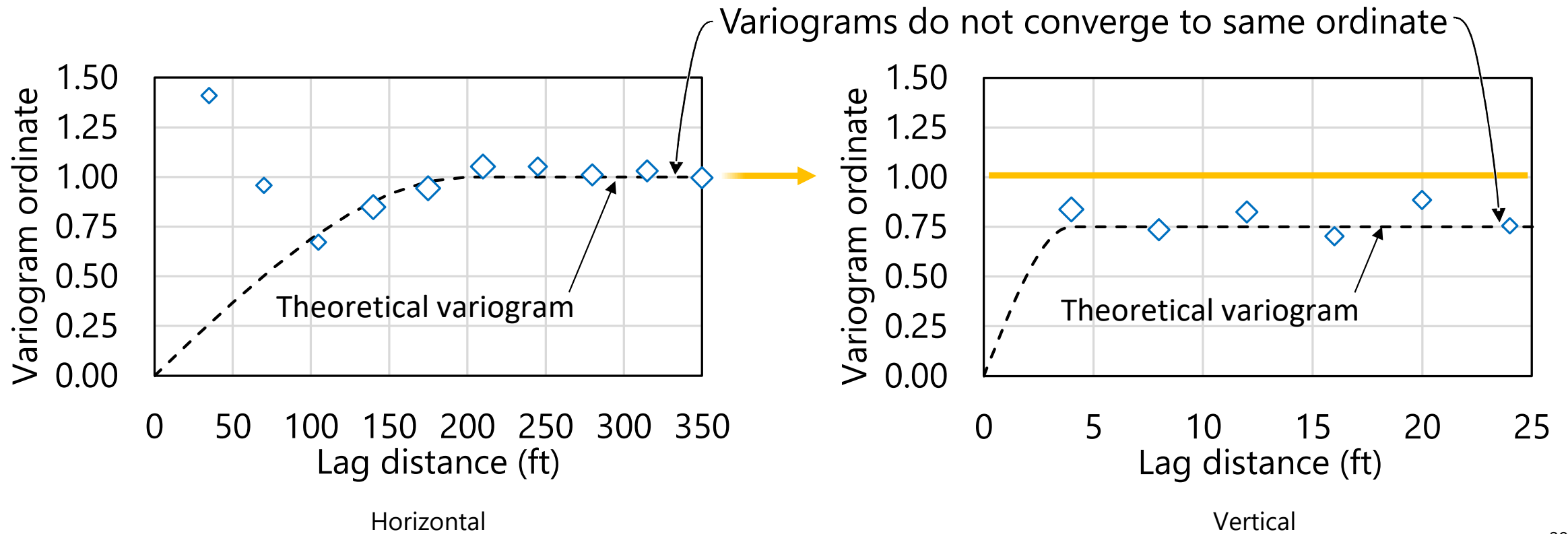
- Example: layer 2





Inspect variograms

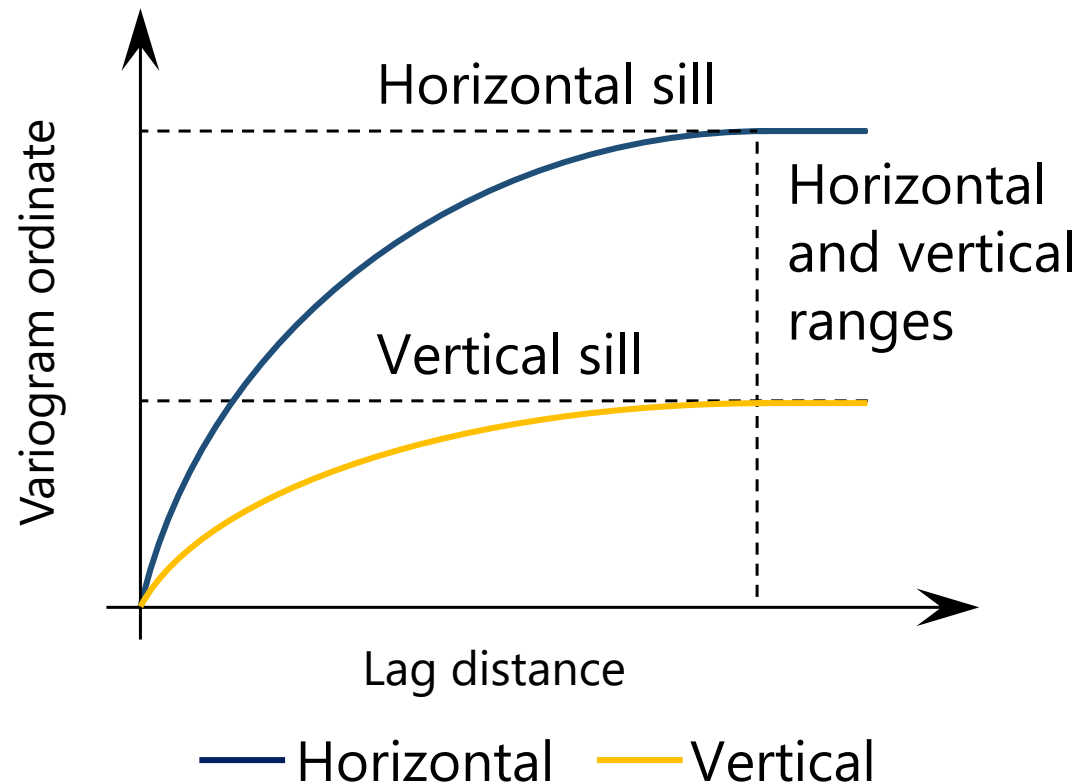
- Example: layer 2





Inspect variograms

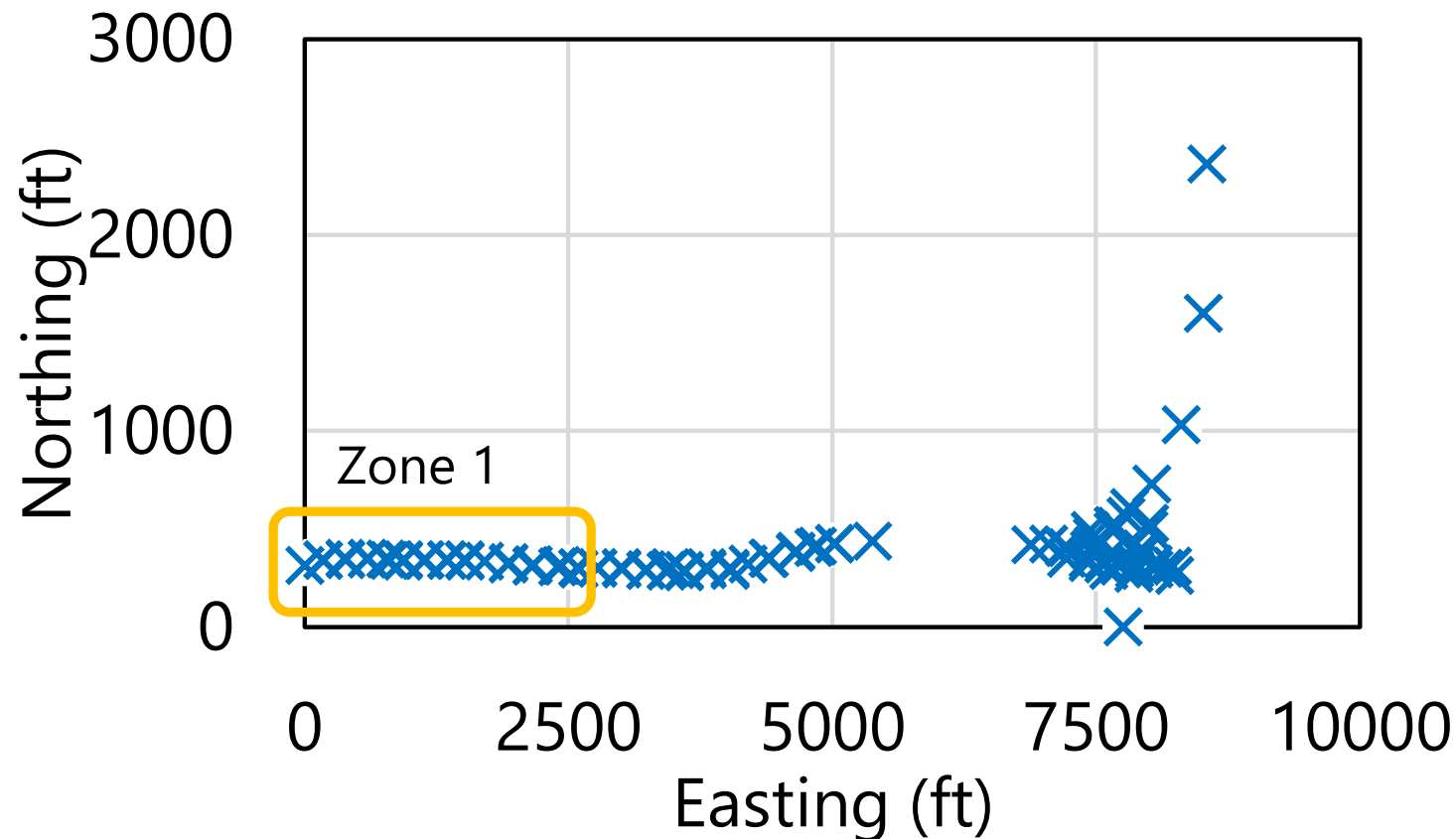
- Recall that variograms can reveal geological zones





Return to plan view of site and select subsets of borings

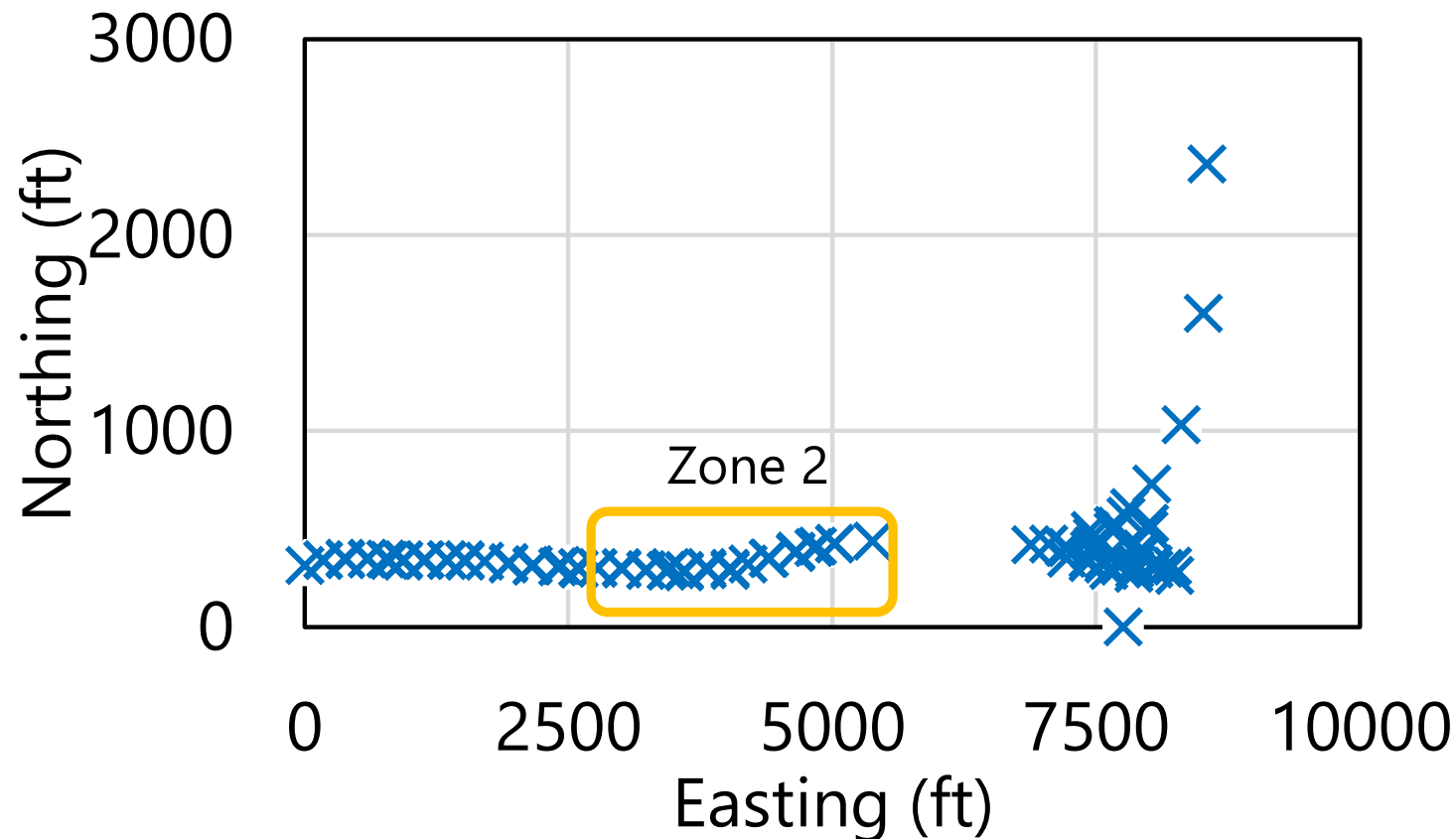
- Example: Western "strip" of 25 borings





Return to plan view of site and select subsets of borings

- Example: Eastern "strip" of 23 borings





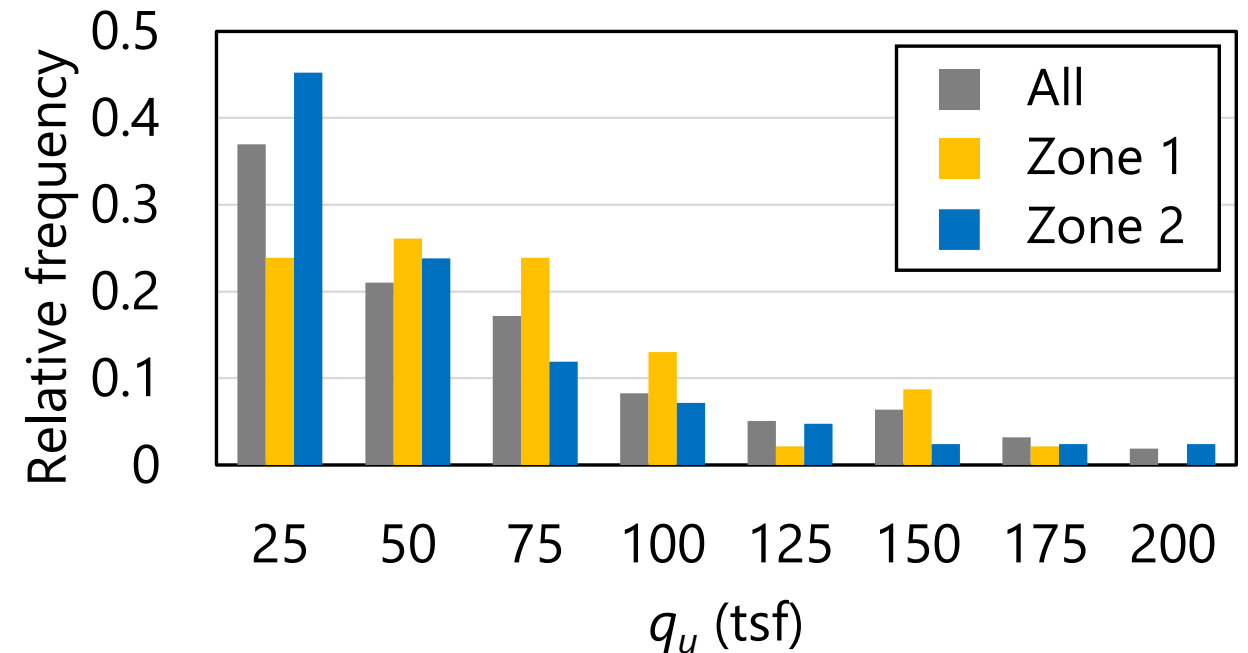
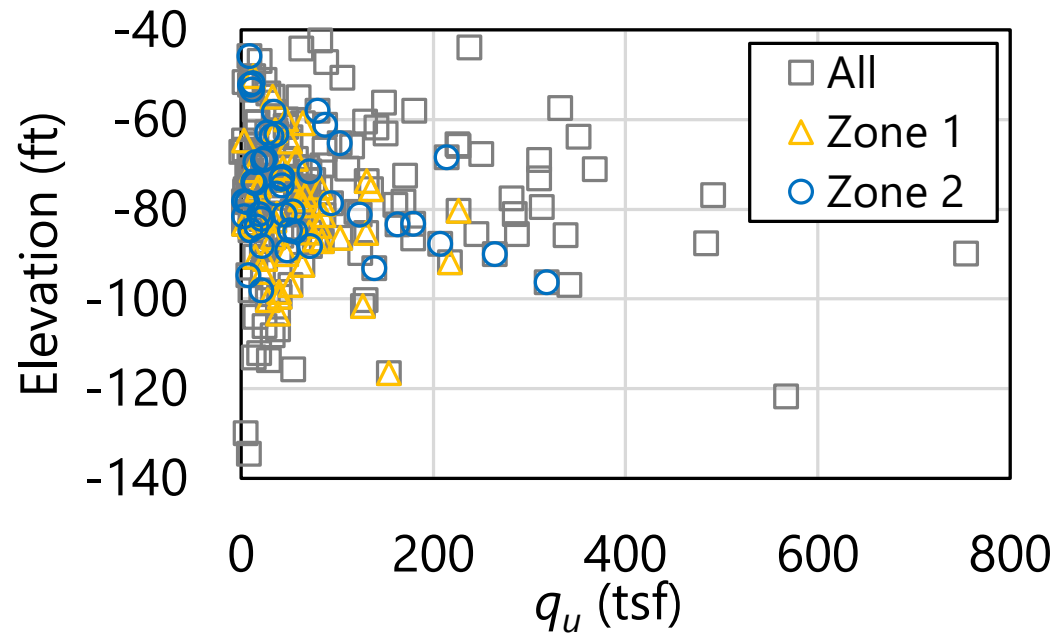
Use geostatistical tool to analyze each zone

- Form (or recheck) layer definitions
- Form variograms
 - Inspect variograms
- Conduct geostatistical simulation
- Incorporate method error
- View elevation profiles of computed axial resistance



Comparison of site-wide vs zonal data

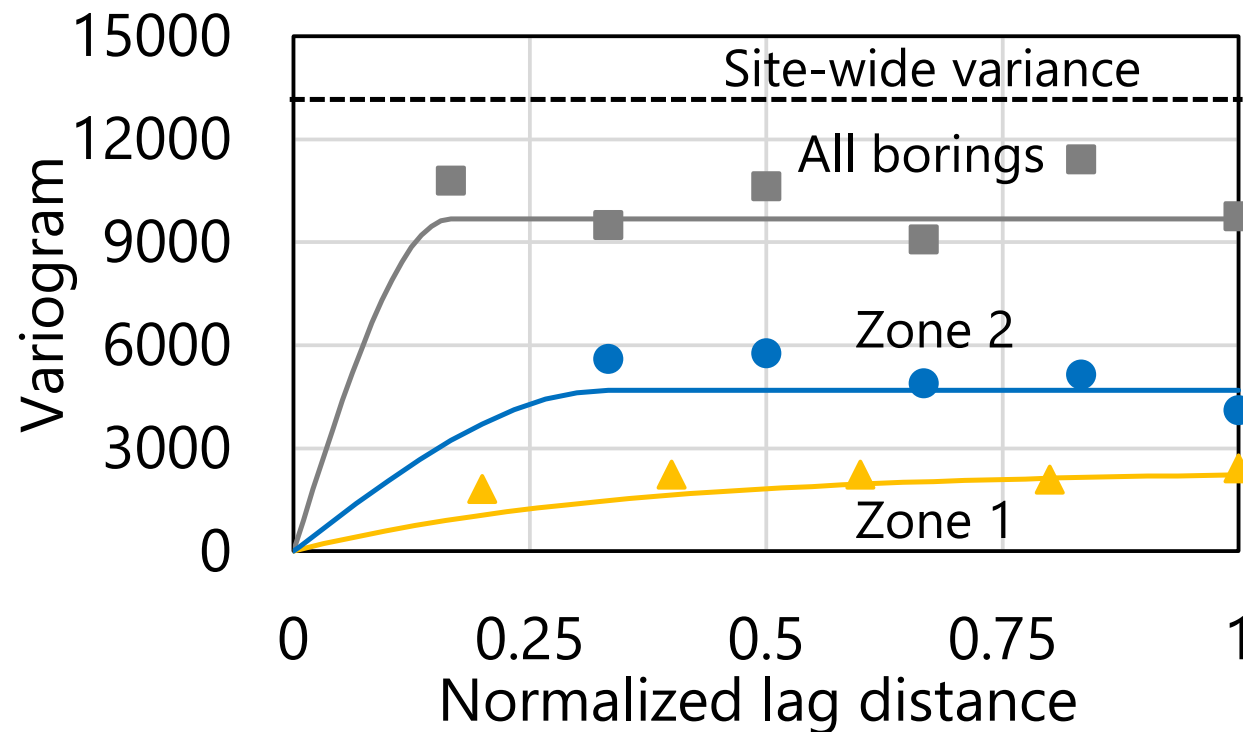
- Example: unconfined compressive strength (q_u) values within layer 2

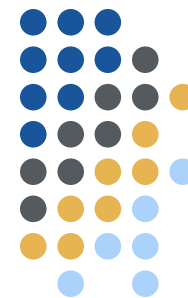




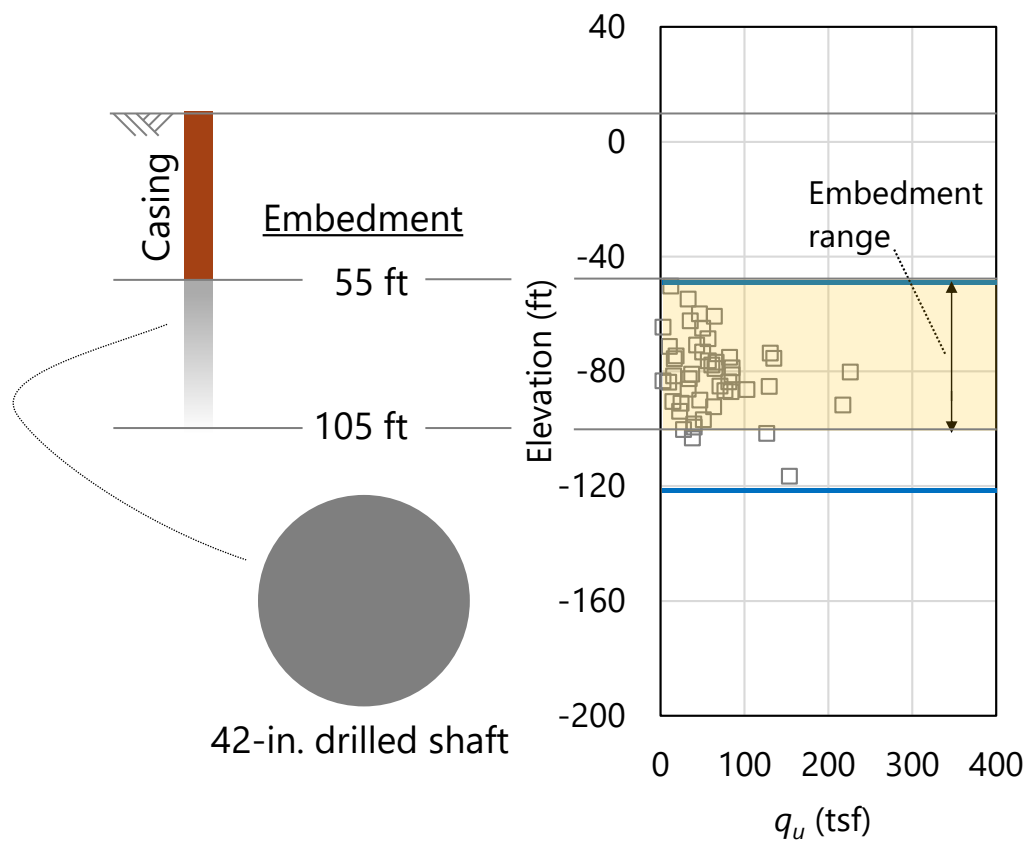
Comparison of site-wide vs zonal variograms

- Example: vertical variograms for layer 2

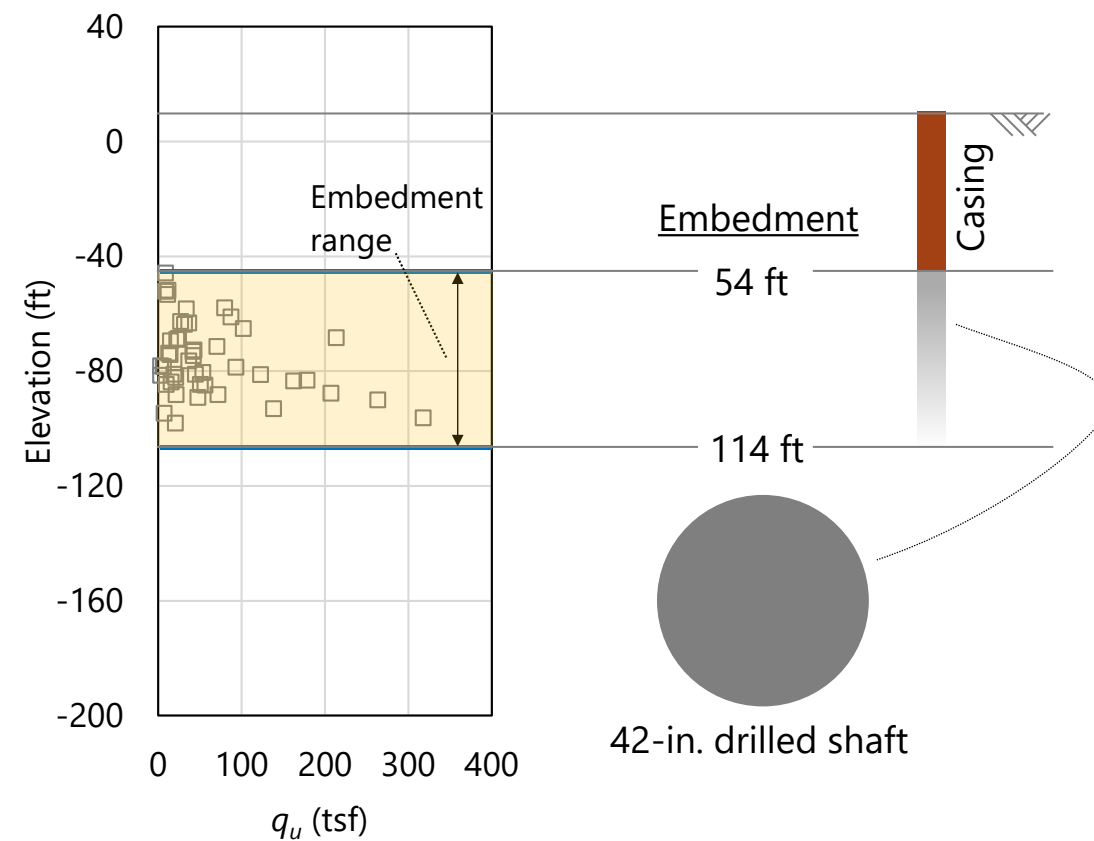




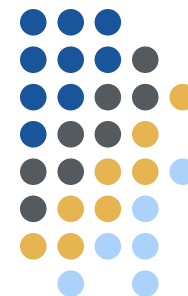
Define drilled shaft diameters and ranges of embedment lengths



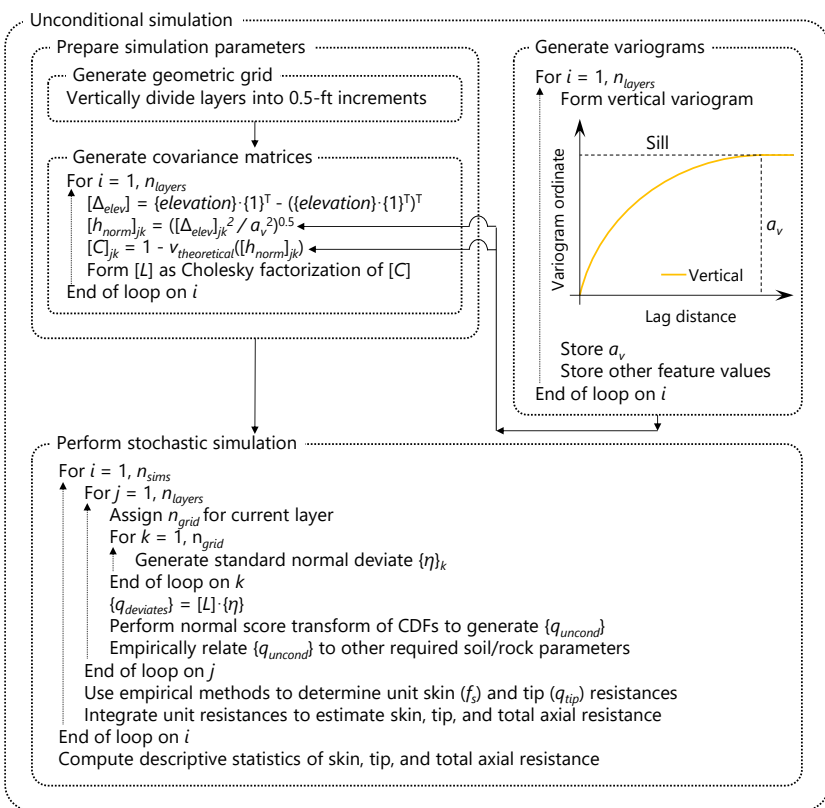
Zone 1



Zone 2



Conduct geostatistical simulation for each zone



Simulation algorithm

File Control Help

Project Information Profile Geostatistics Simulation Spatial Variability Method Error LRFD-Φ

General Geometry

Minimum Length (ft) 75

Maximum Length (ft) 140

Increment (ft) 1

Soil

Ground Surface Elevation (ft) 33.10

Water Table Elevation (ft) 5

Layer Separation

☐ Soil Type 1 (Plastic Clay)

☐ Soil Type 2 (Clay and Silty Sand)

☒ Soil Type 5 (Void)

Unit Weight (pcf)

Cu (tsf)

N (blows/ft)

Simulation

☐ Conditional

☒ Unconditional

Number of Simulations 1500

Boring TS-1

Northing of Foundation (ft)

Easting of Foundation (ft)

Foundation Member Material Properties

Ec (ksi) 4000

Slump (in) 6

Limiting Settlement (%) 1

Unit Weight (pcf) 150

Layer	Mean	Coefficient of Variation	Variance	Sample Count	Vertical Range	Horizontal Range	Horizontal Sill	Detrend
2	91.53	1.24	12916.45	183	4.00	200.00	1.00	Yes

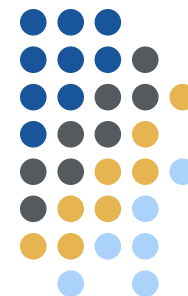
Notes

- The above table is not editable. The values reflect input and calculations carried out on the Profile and Geostatistics pages.
- Only those layers that were assigned a 'Completed' status on the Geostatistics page are displayed in the above table.

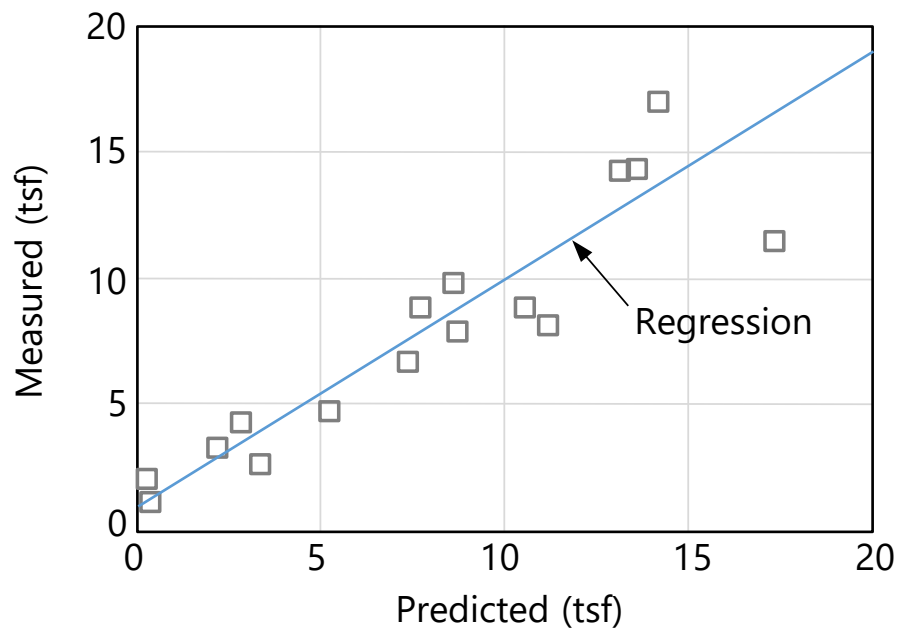
Simulation Status:

Run Simulation

GeoStat – Simulation tab



Incorporate method error



Measured versus predicted side shear resistance for drilled shafts in limestone (McVay et al. 2012)

File Control Help

Project Information Profile Geostatistics Simulation Spatial Variability **Method Error** LRFD-Φ

Driven Pile

☒ Default ☐ Custom

	a	b	CV _e
SPT	0.000	0.000	0.000

Notes

1. Method error calculations for skin friction resistance are based on McVay et al. (2012).
2. Method error calculations for end bearing resistance are based on McVay et al. (2012).

Drilled Shaft

☒ Default ☐ Custom

	a	b	CV _e
Clay	0.000	0.000	0.000
Sand	0.000	0.000	0.000

Notes

1. Method error corrections for skin friction are based on NCHRP 507.
2. Method error corrections for end bearing resistance are based on NCHRP 507.

Limestone

☒ Default ☐ Custom

	a	b	α _e ²
McVay	0.000	0.000	0.000
O'Neill	0.000	0.000	0.000

Notes

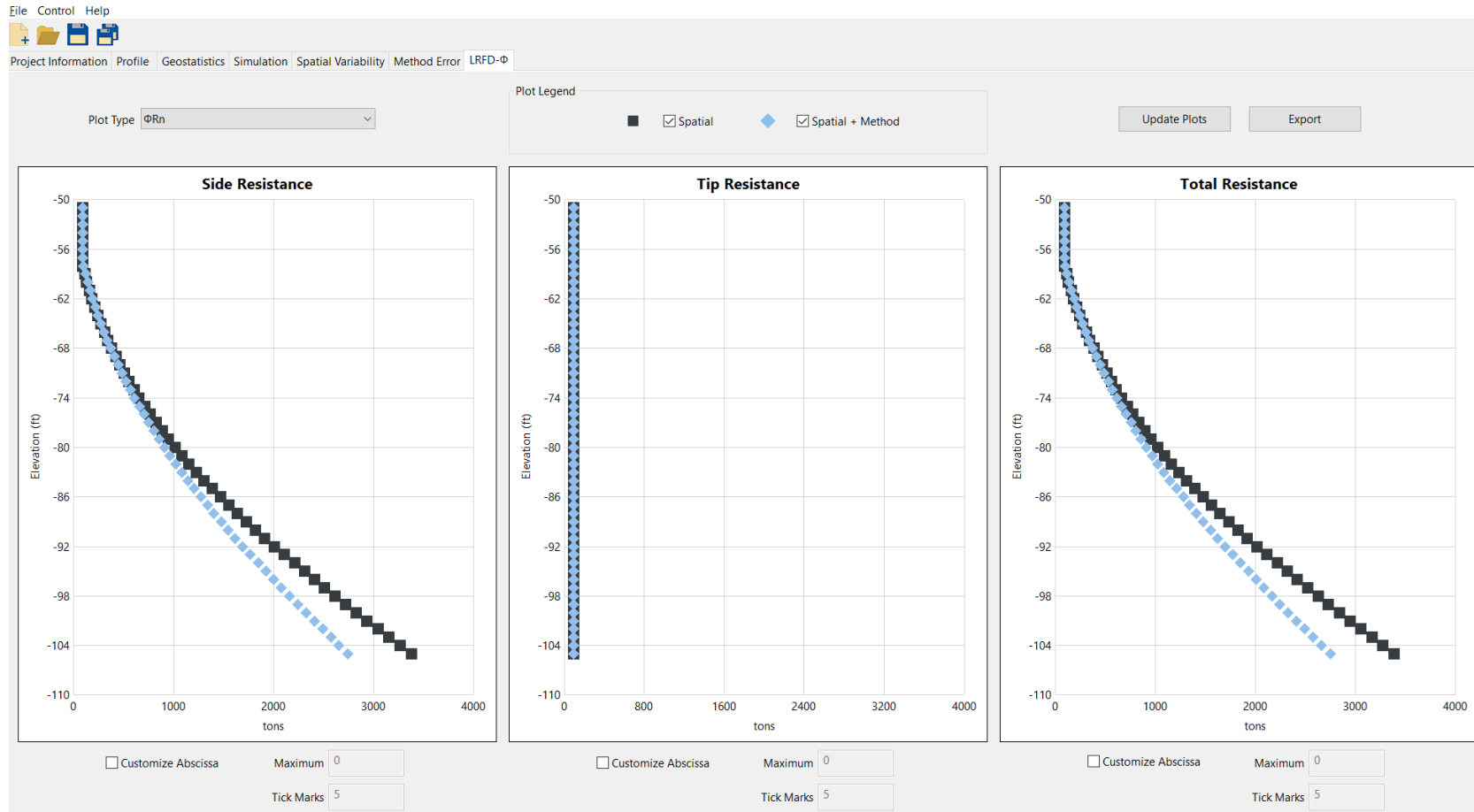
1. Method error corrections for skin friction are based on McVay et al. (2003).
2. Method error corrections for end bearing are based on FHWA-RD-95-172, with a=0.

Process Method Error

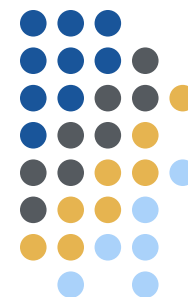
GeoStat – Method Error tab



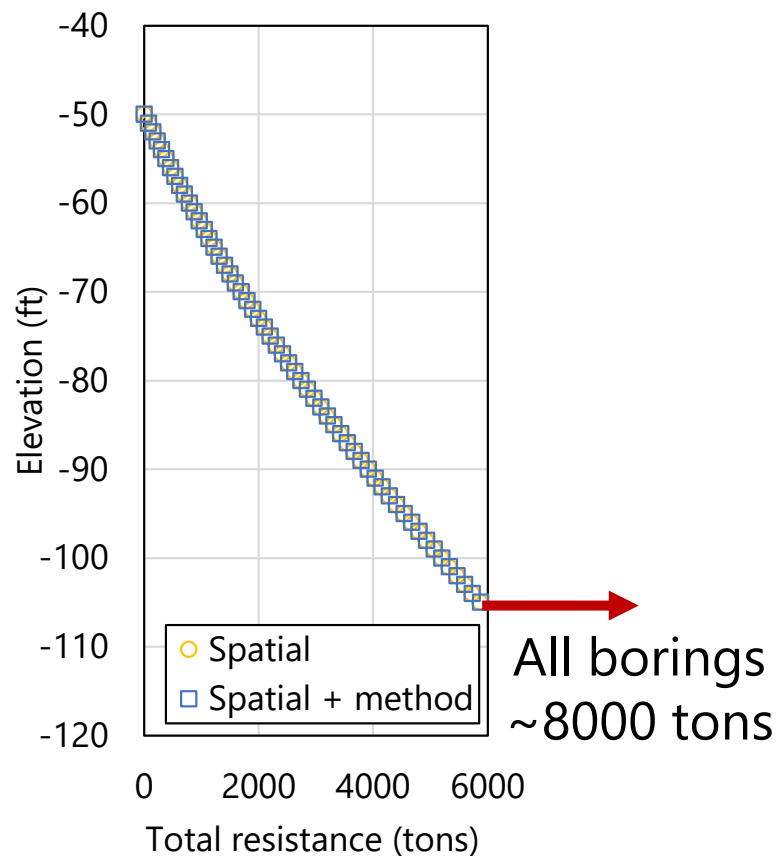
View elevation profiles of computed results



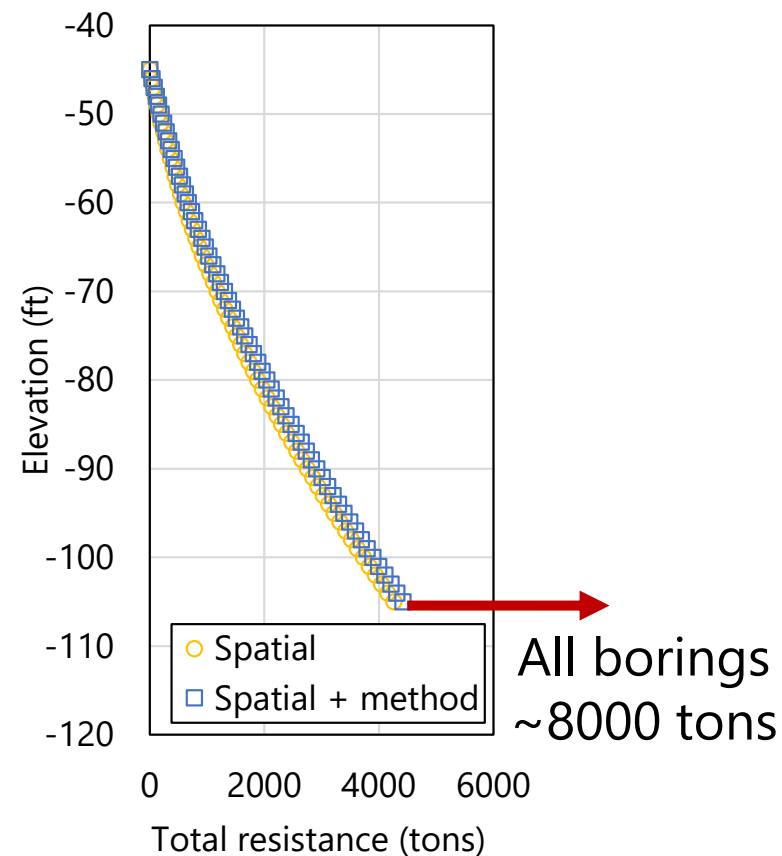
LRFD- ϕ tab for plotting profiles of resistance factors, ϕ , and factored resistances



Computed profiles of unfactored resistance



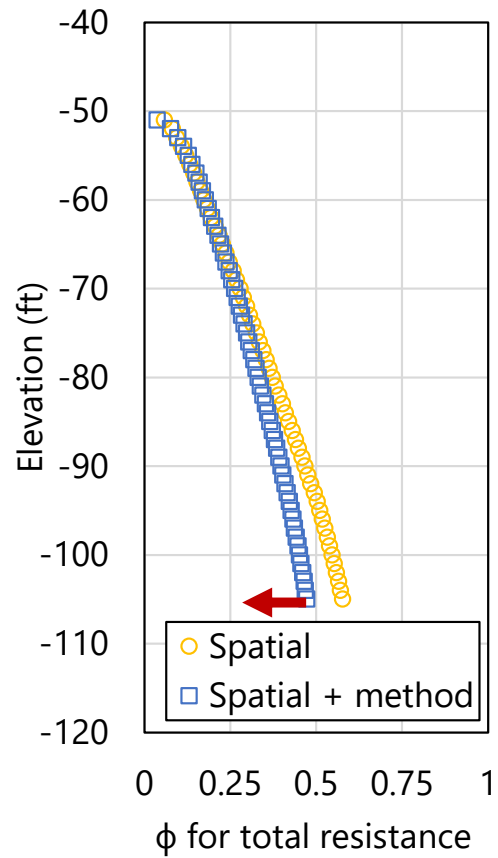
Zone 1



Zone 2

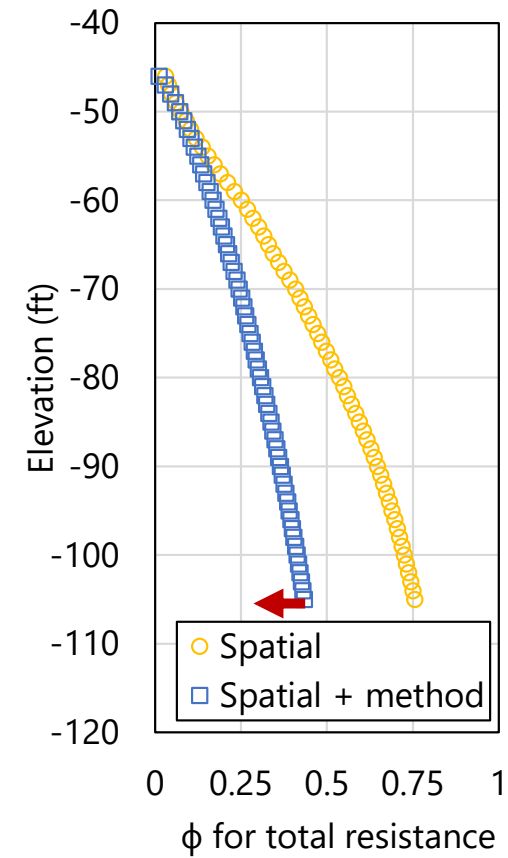


Computed profiles of resistance factor, ϕ



All borings
~0.3

Zone 1

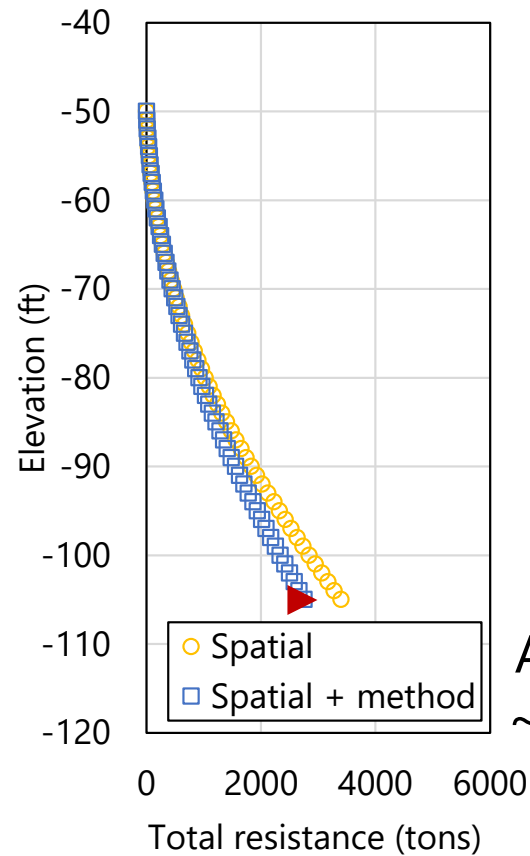


All borings
~0.3

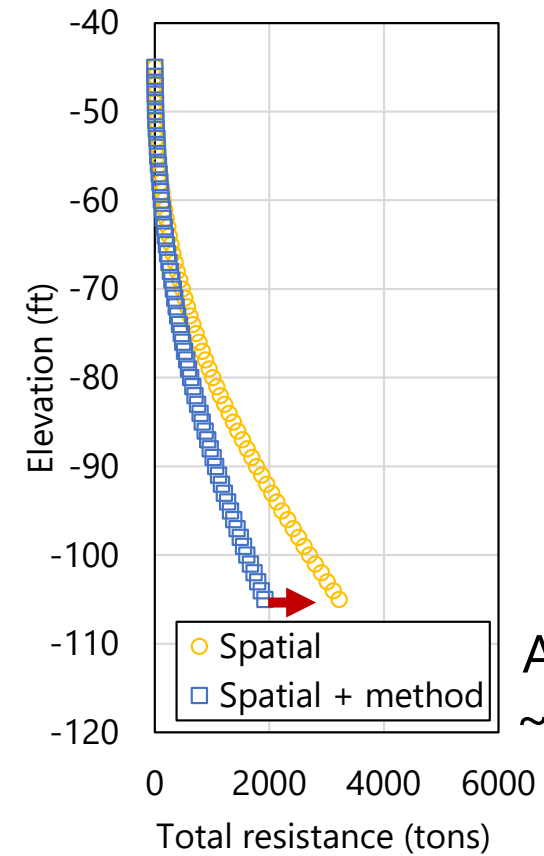
Zone 2



Computed profiles of factored resistance



Zone 1



Zone 2



Outline

- Introduction
- Characterization of spatial variability
- Illustration case
- Summary



Summary

- Spatial variability is intrinsic to site data
- Method error is present in empirical approaches
- Geostatistical design tool has been developed to directly address spatial variability and method error
 - Can be used to compute axial resistance
 - Driven piles
 - Drilled Shafts



Summary

- Benefits of using geostatistical design tool
 - Gauge sufficiency of available geotechnical site investigation data
 - More representative layer definitions
 - Prevent mixing data from different geological zones in axial resistance calculations
 - Compute axial resistance and associated variability/uncertainty
 - Calculate location-specific resistance factors (use must be approved by Owner)
- Additional types of site measurements in development
 - CPT
 - Measuring while drilling (MWD) for drilled shafts in limestone



Thank you

